

Tutorial 3: Solutions

CSC 467 Compilers and Interpreters
Fall Semester, 2005

1. (a) The translation scheme is :

$$\begin{array}{ll}
 S \rightarrow \text{id}:=E & \{ S.\text{type} = \dots, \\
 & \quad S.\text{val} = E.\text{val} \} \\
 S \rightarrow \text{if } E \text{ then } S_1 & \{ S.\text{type} = \dots, \\
 & \quad S.\text{val} = S_1.\text{val} \} \\
 S \rightarrow \text{while } E \text{ do } S_1 & \{ S.\text{type} = \dots, \\
 & \quad S.\text{val} = S_1.\text{val} \} \\
 S \rightarrow S_1 ; S_2 & \{ S.\text{type} = \dots, \\
 & \quad S.\text{val} = S_2.\text{val} \}
 \end{array}$$

- (b) The translation scheme is :

$$\begin{array}{ll}
 E \rightarrow E_1 \text{ B } E_2 & \{ E.\text{type} = \text{if } (E_1.\text{type}=\text{boolean} \text{ and } E_2.\text{type}=\text{boolean}) \\
 & \quad \text{then } E_1.\text{type} \text{ else } \textit{type_error} \} \\
 B \rightarrow \text{and} \mid \text{or} & \{ \} \\
 E \rightarrow \text{not } E_1 & \{ E.\text{type} = \text{if } (E_1.\text{type}=\text{boolean}) \text{ then } E_1.\text{type} \text{ else } \textit{type_error} \} \\
 E \rightarrow E_1 \text{ C } E_2 & \{ E.\text{type} = \text{if } (E_1.\text{type}=E_2.\text{type}) \text{ then } \text{boolean} \text{ else } \textit{type_error} \} \\
 C \rightarrow < \mid > \mid == \mid != & \{ \}
 \end{array}$$

2. **Base case:** When we have only one procedure call, then there is only one activation record. $D[1]$ points to that activation record, so the procedure will see the correct display. **For n calls:** Suppose that at the n th call the procedure called sees the correct display. We will prove the statement for $n + 1$ calls.

For $n + 1$ calls: We have two cases:

- (a) Procedure p at nesting depth i calls procedure q at nesting depth $j > i$. This means that q is nested within p . The first i elements of the display do not change (remain correct) and $D[j]$ (which is actually $D[i + 1]$) points to the new activation record. So q will also see the correct display $D[j]$.
- (b) Procedure p at nesting depth i calls procedure q at nesting depth $j \leq i$. This means that p is nested within q . The first $j - 1$ elements of the display as well as $D[i]$ do not change (remain correct). The old value of $D[j]$ is saved in the new activation record and then $D[j]$ points to the new activation record of q . Therefore, $D[j]$, too, points to the correct activation record and q sees the correct display.
3. (a) The values of i and $A[i]$ remain unchanged.
 (b) `swap2` successfully swaps the values.
 (c) `swap2` successfully swaps the values.
 (d) i is successfully set to $A[i]$ but instead of setting $A[i]$ to i , it sets $A[A[i]]$ to i .
4. (a) D.s

(b) $F.w, F.v, D.v$

(c) Yes, because $D.s$ depends only on attributes of its siblings to its left (in $F \rightarrow FD$) or has no dependencies (in $F \rightarrow D$).

$$F \rightarrow \{D.s = -1\}$$

D

$$\{F.w = 1, F.v = D.v\}$$

$$F \rightarrow F_1$$

(d) $\{D.s = -F_1.w - 1\}$

D

$$\{F.w = F_1.w + 1, F.v = F_1.v + D.v\}$$

$$D \rightarrow 0 \{D.v = 0\}$$

$$D \rightarrow 1 \{D.v = 2^{D.s}\}$$

(e) Only the changes are shown:

$F \rightarrow ND$	$D.s = N.s$
$N \rightarrow \epsilon$	$N.s = -1$
$F \rightarrow F_1MD$	$M.i = F_1.w$
	$D.s = M.s$
$M \rightarrow \epsilon$	$M.s = -M.i - 1$