

Novel Flow Control for Fully Adaptive Routing in Cache-coherent NoCs

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Supplementary file

Abstract—This paper contains the supplementary material to the paper submitted to IEEE TPDS entitled “Novel Flow Control for Fully Adaptive Routing in Cache-coherent NoCs” (labeled as “main file” in this paper). In Sec. 1, we prove that if a routing algorithm with WPF is deadlock-free, then this algorithm with conservative VC re-allocation is also deadlock-free. In Sec. 2, we provide further insights for the performance trends of routing algorithms by analyzing the buffer utilization. In Sec. 3, we present the full system performance analysis. In Sec. 4, we show the recursive algorithm to calculate the allowable escape VC. In Sec. 5, we perform sensitivity study on several configuration parameters. In Sec. 6, we provide further discussion about the designs.

1 LOGICAL EQUIVALENCE OF Alg AND $Alg+WPF$

Sec. 4.1 proposes Theorem 1, which declares that if a fully adaptive routing algorithm with conservative VC re-allocation (named as Alg) is deadlock-free, then applying WPF on this routing algorithm (named as $Alg+WPF$) is also deadlock-free. This section proves that if $Alg+WPF$ is deadlock-free, then Alg is deadlock-free as well. In addition to Assumption 1 in Sec. 4.1 of the main file, this proof needs another simple assumption about the routing algorithm.

Assumption 2. The definition of a routing algorithm is independent of the packet length.

Assumption 2 implies that if two packets are injected from the same source and destined to the same node, they can use the same set of VCs even though these packets have different lengths. This assumption is generally used in many previous theories [2], [3], [6], [7], [8], [9], [10], [12], [18], [21], [24], [25]. We prove the following theorem.

Theorem 3: If $Alg+WPF$ is deadlock-free, then Alg is also deadlock-free.

Description: This proof is similar to the proof of Theorem 1 in the main file. We prove that if Alg has a deadlock configuration, then $Alg+WPF$ has a deadlock configuration as well. Use $Config_0$ in Fig. 1 as an example. We replace packet P_i with packet P'_i to completely fill all VCs. The source and destination of P'_i are the same as P_i , while P'_i may have more flits than P_i to completely fill the VCs. We prove

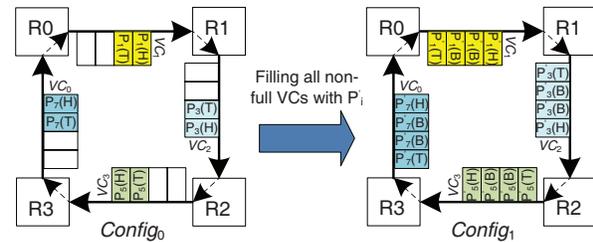


Fig. 1. The construction of a new configuration.

that $Alg+WPF$ can achieve $Config_0$, and $Config_0$ is a deadlock configuration. However, $Alg+WPF$ is deadlock-free, thus there is no such configuration.

Proof: By contradiction. If Alg is not deadlock-free, then there is a deadlock configuration ($Config_0$) in which a set of packets, P_{set_0} , are waiting on VCs held by other packets in P_{set_0} . We prove that there is a deadlock configuration for $Alg+WPF$ in three steps.

Step 1: We build a new configuration based on $Config_0$. Consider each packet P_i in P_{set_0} . If P_i does not completely fill all VCs where its flits reside, we replace P_i with packet P'_i to completely fill all VCs occupied by P_i . The source and destination of P'_i are the same as P_i , and the length of P'_i is larger than P_i . If P_i completely fills all VCs where its flits reside, P'_i is the same as P_i . We label the new configuration as $Config_1$, and the set of packets in $Config_1$ as P_{set_1} .

Step 2: We prove that when the network is routed by $Alg+WPF$, all packets in P_{set_1} can move to their current VCs in $Config_1$, and the head flits of these packets are at VC heads. For each packet P'_i in P_{set_1} , we consider its corresponding packet P_i in $Config_0$. We further consider each hop hop_k of P_i when it is routed by Alg . Assume the head flit of P_i moves to VC_k 's head during hop_k . The routing algorithm allows P_i to use VC_k . Although P'_i and P_i may have different packet lengths, they have the same source and destination information. Based on Assumption 2, the routing algorithm allows P'_i to use VC_k as well.

Since $Alg+WPF$ is deadlock-free, VC_k must become available at some time. Based on Assumption

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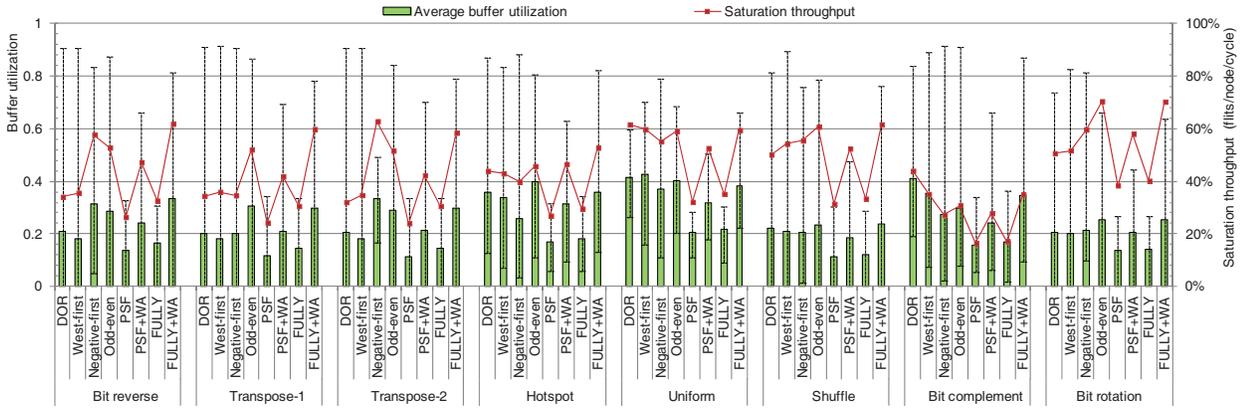


Fig. 2. The buffer utilization and throughput in saturation for several routing algorithms.

1 in the main file, P'_i has some possibility to request VC_k . There are two cases when P'_i requests VC_k .

2.1) VC_k is empty. VC_k can be re-allocated to P'_i with conservative VC re-allocation. Thus, the head flit of P'_i will move to VC_k 's head.

2.2) VC_k is not empty. But VC_k already received the tail flit of last allocated packet and still has enough buffers for P'_i . WPF can re-allocate VC_k to P'_i . Yet, when P'_i reaches VC_k , its head flit is not at VC_k 's head. Considering $Alg+WPF$ is deadlock-free, the packets in VC_k before P'_i must be sent out in limited time. Then, the head flit of P'_i is at VC_k 's head.

Considering 2.1) and 2.2) together, if the head flit of P_i moves to the head of a VC during any hop when routed by Alg , the head flit of P'_i can also move to the same VC head when routed by $Alg+WPF$. Thus, when routed by $Alg+WPF$, P'_i can be routed to its current VC(s) in $Config_1$, and the head flit of P'_i is at the VC head.

Step 3: We prove that $Config_1$ is a deadlock configuration for $Alg+WPF$. Since all VCs in $Config_1$ are completely filled, all packets in P_{set_1} still wait for VCs held by other packets in P_{set_1} , even with WPF applied. $Config_1$ is a deadlock configuration for $Alg+WPF$. But $Alg+WPF$ is deadlock-free, so there is no deadlock configuration. Thus, Alg is deadlock-free as well. \square

Theorem 1 of the main file declares that if Alg is deadlock-free, then $Alg+WPF$ is deadlock-free as well. Theorem 3 declares that if $Alg+WPF$ is deadlock-free, then Alg is deadlock-free as well. Considering these two theorems together, the deadlock freedom of $Alg+WPF$ is logically equivalent to the deadlock freedom of Alg . Therefore, the WPF optimization of traditional wormhole flow control does not have any influence on the deadlock freedom.

2 BUFFER UTILIZATION OF ROUTING ALGORITHMS

Sec. 5.1 of the main file measures the performance of several fully adaptive, partially adaptive and deterministic routing algorithms. This section provides further insights of the performance trends by analyzing

the buffer utilization of all evaluated designs. Fig. 2 illustrates the average buffer utilization of all network VCs in saturation for eight synthetic traffic patterns. The maximum and minimum rates are given by the error bars. Fig. 2 also shows the saturation throughput supported by routing algorithms. There are several important insights.

First, buffers are used to support high throughput. The saturation throughput of routing algorithms is related to the buffer utilization. Higher average buffer utilization generally leads to higher saturation throughput. This trend is obvious in bit complement. Bit complement sends traffic from node $\{s_3, s_2, s_1, s_0\}$ to node $\{-s_3, -s_2, -s_1, -s_0\}$, which has the largest average hop count [14], and puts the highest pressure on the buffers among all evaluated traffic patterns.

Second, for the same routing algorithm in different traffic patterns, there may be fluctuations between the buffer utilization and the saturation throughput. For example, even though DOR shows much higher buffer utilization for bit complement than shuffle, its saturation throughput for bit complement is lower than shuffle. These fluctuations are due to that the same routing algorithm uses different VCs for different patterns; the network becomes saturated in different status. Similarly, since some algorithms use different VCs in the same traffic pattern, there may be slight fluctuations as well. For example, even though the average buffer utilization of west-first is slightly lower than DOR for bit reverse, its saturation throughput is higher than DOR.

Third, since all fully adaptive routing algorithms, including PSF, PSF+WA, FULLY and FULLY+WA, use the same set of VCs for the same traffic pattern, their saturation throughput is roughly proportional to the buffer utilization. For instance, in bit reverse, PSF+WA's average buffer utilization is 78.3% higher than PSF, making it perform 79.5% better than PSF. Similarly, PSF+WA has 67.4% higher average buffer utilization than PSF in shuffle, and its saturation throughput is 67.2% higher than PSF.

Fourth, the network becomes saturated when some resources become saturated [4]. For most patterns and

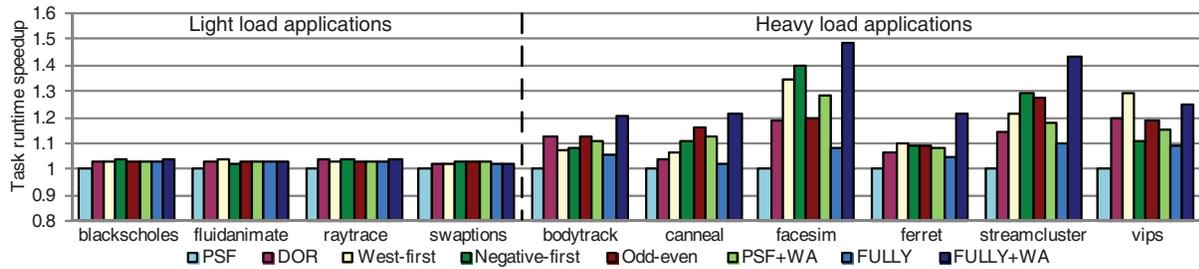


Fig. 3. System speedup for PARSEC benchmarks.

most algorithms, the bottleneck is VCs; networks become saturated when some VCs have more than 80% utilization, including DOR, west-first, negative-first and odd-even in most patterns. When the algorithm provides abundant adaptiveness, it distributes traffic more uniformly among VCs, preventing them from becoming the bottleneck. Instead, the bottleneck may be the crossbar or network interface [23]. For example, since negative-first offers adaptiveness for all traffic in transpose-2, the network becomes saturated even when the maximum buffer utilization is only 49.2%. Similarly, when in saturation, the maximum buffer utilization of PSF+WA and FULLY+WA is lower than partially adaptive routing and DOR.

Fifth, PSF and FULLY are limited by conservative VC re-allocation; their maximum buffer utilization for evaluated patterns is less than 40%. Applying WPF on adaptive VCs and aggressive VC re-allocation on escape VCs greatly increases buffer utilization, which proportionally improves performance. FULLY supports higher routing flexibility than PSF, which brings higher buffer utilization and performance.

3 EVALUATION ON PARSEC WORKLOADS

3.1 Methodology and Configuration

To measure full-system performance, we leverage FeS2 [16] for x86 simulation and BookSim for NoC simulation. FeS2 is implemented as a module for Simics [15]. We run PARSEC benchmarks [1] with 16 threads on a 16-core CMP, which is organized as a 4×4 mesh. Prior research shows the frequency of simple cores in a many-core platform can be optimized to 5~10 GHz, while the frequency of NoC router is limited by the allocator speed [5]. We assume cores are clocked $5 \times$ faster than the network. Cache lines are 64 bytes; long packets are 5 flits long with a 16-byte flit width. We use a distributed, directory-based MOESI coherence protocol which needs 4 VNs for protocol-level deadlock freedom. Each VN has 2 VCs; each VC is 4 flits deep. The router pipeline is the same as described in Sec. 4.4 of the main file. All benchmarks use the *sims*small input sets. The total runtime is the performance metric. TABLE 1 gives the system configuration.

3.2 Performance

Fig. 3 shows the speedups relative to PSF for PARSEC workloads. We divide the 10 applications into 2 classes. For blackscholes, fluidanimate, raytrace

TABLE 1. Full system simulation configuration.

# of cores	16, 4×4 Mesh
L1 cache (D & I)	private, 4-way, 32KB each
L2 cache	private, 8-way, 512KB each
Cache coherence	MOESI distributed directory

and swaptions, different algorithms perform similarly. The working sets of these applications fit into the caches and their computation phases consist of few synchronization points, leading to a lightly loaded network. The system performance of these applications is unaffected by techniques that improve the network throughput, such as sophisticated routing algorithms.

However, the routing algorithms affect the other 6 applications. These applications have heavier loads than previous 4 applications. Yet, their average aggregate loads during the running periods are lower than the network saturation points. The highest average aggregate injection rate for canneal is 12.3% flits/node/cycle, which is below the saturation points for all designs. Two factors bring performance improvements for these 6 applications. First, these applications exhibit period bursty communication and the synchronization primitives create one hotspot inside the network. The bursty communication and the hotspot make the network operate past saturation at times during the running period. Thus, these applications benefit from routing algorithms with higher throughputs. Second, short packets are critical in cache-coherent many-core platforms; they carry time-critical control messages that are often on the application's critical path. These short packets can affect the execution time significantly. The novel flow control reduces the packet latency, especially under heavy loads, which brings performance gains. For example, FULLY+WA has 48.5% and 43.0% speedups over PSF for facesim and streamcluster.

Since most of vips application's bursty communication is eastbound, west-first performs best for vips. For facesim and streamcluster, negative-first offers higher adaptiveness than odd-even, thus achieving better performance. For all heavy load applications except vips, FULLY+WA performs best. Across these applications, FULLY+WA achieves an average of 21.3% and maximum 37.8% speedup over FULLY. With sufficient flexibility, FULLY+WA has an average 12.1% speedup over PSF+WA. The average speedups of FULLY+WA are 29.3%, 15.0%, 10.1%,

```

void AllowableEVCs(int cx,int cy,int dx,int dy,
int*** EVCs){
  if( cx == dx && cy == dy ){ // destination
return;
} else if( cx < dx && cy == dy ){ // east
EVCs[cx+1][cy][1] = 1;
AllowableEVCs( cx+1, cy, dx, dy, EVCs );
} else if( cx > dx && cy == dy ){ // west
EVCs[cx-1][cy][0] = 1;
AllowableEVCs( cx-1, cy, dx, dy, EVCs );
} else if( cx == dx && cy < dy ){ // north
EVCs[cx][cy+1][3] = 1;
AllowableEVCs( cx, cy+1, dx, dy, EVCs );
} else if( cx == dx && cy > dy ){ // south
EVCs[cx][cy-1][2] = 1;
AllowableEVCs( cx, cy-1, dx, dy, EVCs );
} else if( cx>dx && cy>dy ){ // north-west
EVCs[cx-1][cy][0] = 1;
AllowableEVCs( cx-1, cy, dx, dy, EVCs );
AllowableEVCs( cx, cy-1, dx, dy, EVCs );
} else if( cx>dx && cy<dy ){ // south-west
EVCs[cx-1][cy][0] = 1;
AllowableEVCs( cx-1, cy, dx, dy, EVCs );
AllowableEVCs( cx, cy+1, dx, dy, EVCs );
} else if( cx<dx && cy>dy ){ // north-east
EVCs[cx+1][cy][1] = 1;
AllowableEVCs( cx+1, cy, dx, dy, EVCs );
AllowableEVCs( cx, cy-1, dx, dy, EVCs );
} else if( cx<dx && cy<dy ){ // south-east
EVCs[cx+1][cy][1] = 1;
AllowableEVCs( cx+1, cy, dx, dy, EVCs );
AllowableEVCs( cx, cy+1, dx, dy, EVCs );
}
}

```

Fig. 4. The AllowableEVCs algorithm. The initial value of EVCs is 0s. cx and cy are X and Y positions of the current node. dx and dy are X and Y positions of the destination. Port encoding: East: 0, West: 1, South: 2, North: 3.

9.9% and 10.4% over PSF, DOR, west-first, negative-first and odd-even, respectively.

4 ALLOWABLE ESCAPE VCS (EVCs)

In Sec. 5.2 of the main file, we leverage a recursive algorithm to calculate the allowable escape VCs (EVCs) for synthetic traffic patterns. Here, we present the algorithm, as shown in Fig. 4.

This algorithm recursively calculates all allowable EVCs for a packet sent from node (cx, cy) to node (dx, dy) . At each step, the algorithm marks the escape VC at the port which adheres to DOR as allowable by setting the corresponding element of *EVCs* array to '1'. Fully adaptive routing may forward the packet to all neighbors inside the minimum quadrant defined by the current position and the destination. At the next step, the algorithm continues by using these neighbors as current positions. For example, if $cx > dx$ and $cy > dy$, then the destination is at the north-west quadrant of current position. The EVC at the east input port of node $(cx - 1, cy)$ is allowed to be used. The packet may move to node $(cx - 1, cy)$ and node $(cx, cy - 1)$, and the algorithm continues by using them as current positions at the next step. By considering all source and destination pairs defined in the traffic pattern, we get the allowable EVCs in a 4×4 mesh network, as shown in TABLE 4 of the main file.

5 SENSITIVITY TO NETWORK DESIGN

This section performs sensitivity study for network configuration parameters. Except for the analyzed

TABLE 2. Baseline configuration and variations.

Characteristic	Baseline	Variations
Topology (mesh)	4×4	8×8
VCs/VN	2	4
Flit buffers/VC	4	3, 2
SFP ratio	80%	60%, 40%

parameter, other parameters are the same as the baseline configuration shown in TABLE 2. This section makes comparison with the performance of baseline configuration shown in the main file. To improve the readability, we reproduce Fig. 10 of the main file, as shown in Fig. 5 here.

5.1 Single-flit Packet Ratio (SFP ratio)

Single-flit packet (SFP) ratios depend on the cache hierarchy, the coherence protocol and the application. To test the robustness of our design, we evaluate 60% and 40% SFP ratios for transpose-1. As shown in Fig. 6, DOR, west-first, negative-first and odd-even exhibit nearly identical performance for different SFP ratios. The aggressive VC re-allocation makes their performance insensitive to the packet length distribution. However, the performance of PSF and FULLY improves as the SFP ratio shrinks. Their conservative VC re-allocation favors long packets which utilize buffers more efficiently than short ones. As the SFP ratio decreases, so does the possibility of applying WPF. Thus, the performance gap between FULLY+WA and FULLY (or PSF+WA and PSF) decreases. However, even with a 40% SFP ratio, FULLY+WA achieves a 53.1% saturation throughput gain over FULLY.

5.2 VC Depth

Different NoCs may use different VC depths. To test the flexibility, we evaluate 3- and 2-flit deep VCs with bit reverse traffic. Comparing 4 flits/VC (Fig. 5a) and 3 flits/VC (Fig. 7a), DOR and west-first perform similarly, while FULLY and PSF show minor performance degradation. DOR and west-first offer no or very limited adaptiveness which is a major factor in their performance. Thus, reducing the VC depth from 4 to 3 has little effect. The bottleneck of FULLY and PSF is conservative VC re-allocation. Considering the majority of short packets, reducing the VC depth from 4 to 3 only affects performance slightly. However, the performance of FULLY+WA, PSF+WA, odd-even and negative-first declines with shallower VCs since the VC depth is their bottleneck. Shallow VCs increase the number of hops that a blocked packet spans, which increases the effect of chained blocking [23].

Comparing 3 and 2 flits/VC, performance drops for all algorithms. FULLY outperforms DOR and west-first with 2 flits/VC. As the VC depth decreases, the difference between aggressive and conservative VC re-allocation declines; FULLY gets a relative gain. Even with 2 flits/VC, WPF still optimizes the performance since short packets dominate traffic. In Fig. 7b, FULLY+WA performs 46.2% better than FULLY. Novel flow control leads to superior performance even with

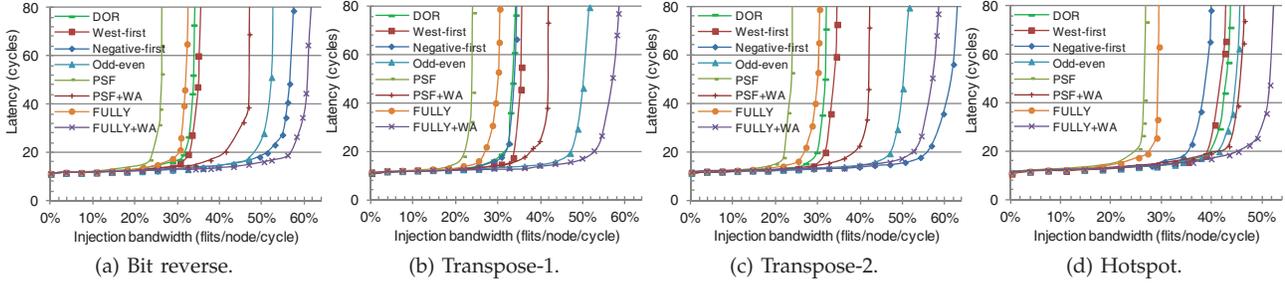


Fig. 5. Routing algorithm performance for the baseline configuration (A reproduction of Fig. 10 in the main file).

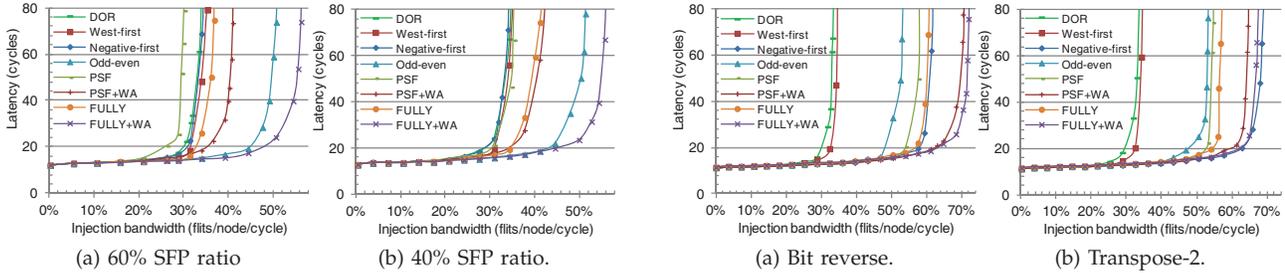


Fig. 6. The performance with different SFP ratios for transpose-1 traffic.

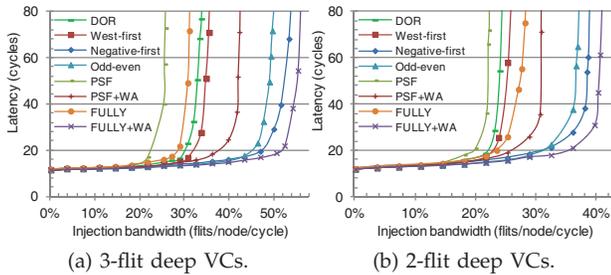


Fig. 7. The performance with different VC depths for bit reverse traffic.

half of the buffers, which enables the design of a low-cost NoC. With 2 flits/VC (Fig. 7b), FULLY+WA's saturation throughput is 40.3%, while FULLY's saturation throughput is 32.3% with 4 flits/VC (Fig. 5a). The same is true for PSF+WA.

5.3 VC Count

Semiconductor scaling and coherence protocol optimization may allow a VN to be configured with more VCs. Comparing 4 VCs/VN (Fig. 8a) and 2 VCs/VN (Fig. 5a), the performance of DOR, west-first and odd-even is almost the same. These algorithms offer limited adaptiveness; although additional results show increasing the VC count from 1 to 2 improves performance, increasing the VC count from 2 to 4 cannot reduce the physical path congestion and does not further improve performance. Negative-first has a modest gain. In contrast, PSF, FULLY, PSF+WA and FULLY+WA all have significant gains; more VCs mitigate the negative effects of conservative VC reallocation. The gap between PSF and FULLY (or PSF+WA and FULLY+WA) decreases with more VCs; more VCs reduce the possibility of using escape VCs in PSF which forces packets to lose adaptivity.

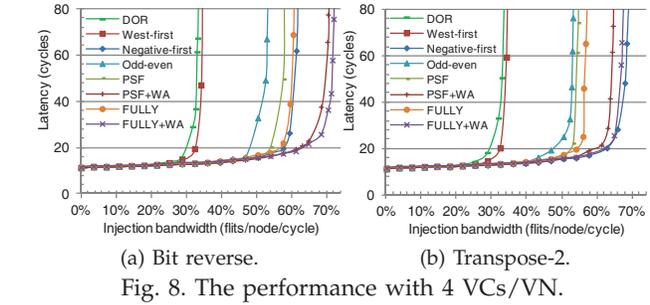


Fig. 8. The performance with 4 VCs/VN.

Fig. 8b shows the performance of transpose-2, which is a favorable pattern for negative-first. FULLY+WA performs similarly to negative-first; with more VCs, the effect of restricting the use of escape VCs in FULLY+WA declines. More VCs reduces the gap between FULLY and FULLY+WA (or PSF and PSF+WA), since the possibility of facing empty VCs increases. Furthermore, using WPF to forward entire packets into non-empty VCs may result in Head-of-Line (HoL) blocking [4] and limit FULLY+WA (or PSF+WA). Nevertheless, FULLY+WA still shows an average 19.8% gain over FULLY for these two patterns with 4 VCs; providing high VC utilization outweighs the negative effect of HoL blocking in a VC-limited NoC. Similar to VC depth, with only 2 VCs, FULLY+WA performs similarly or even better (Figs 5a and 5b) than FULLY with 4 VCs (Fig. 8). WPF provides similar or higher performance with half as many VCs.

5.4 Network Size

Fig. 9 explores the scalability for an 8×8 mesh. The trends across different algorithms are similar to the 4×4 mesh (Fig. 5). Communication is mostly determined by the traffic pattern. Since a larger network leads to higher average hop counts [14], it puts more pressure on VCs than a smaller one. Novel flow control achieves more gains in a larger network. The average improvement for these two patterns of FULLY+WA over FULLY is 108.2%, while it is 93.1% in a 4×4 mesh. As packets travel more hops in a larger network, the possibility of entering an escape VC increases. For PSF and PSF+WA, once the packet enters an escape VC, it loses adaptivity in subsequent hops. Therefore, the gap between FULLY+WA and PSF+WA (or FULLY and PSF) increases with a larger

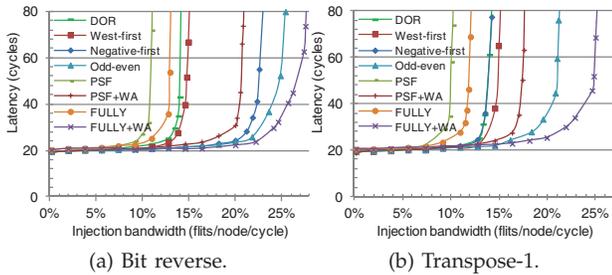


Fig. 9. The performance for an 8×8 mesh network.

network; providing routing flexibility becomes more important with a larger network.

6 FURTHER DISCUSSION

6.1 Packet Length

Packet lengths for cache coherence traffic typically have a bimodal distribution. However, optimizations such as cache line compression [5], [11] create packet distributions that are not bimodal; the packet length may be distributed between a single flit and the maximum flits per packet supported by the architecture. To apply WPF on such NoCs, more downstream VC status registers are needed for the first-stage arbiters shown in Fig. 9 of the main file. An important consideration is how many different packet lengths to apply WPF to. The longest packet length that can use WPF is one flit shorter than the VC depth. Designers can ignore long packets, since there are few opportunities to apply WPF on long packets. This tradeoff depends on the packet length distribution, VC depth, hardware overhead and the expected performance gain.

6.2 DAMQ and Hybrid Flow Controls

Previous research proposed dynamically allocated multi-queue (DAMQ) designs for both off-chip [22] and on-chip networks [17], [26] to improve VC utilization. Even with DAMQ, allowing multiple packets to reside in one VC may lead to deadlock similar to Fig. 3 of the main file for fully adaptive routing in wormhole networks. WPF is complimentary to DAMQ as it ensures deadlock-freedom. WPF can be viewed as a hybrid mechanism combining wormhole and VCT. There are some hybrid flow controls [13], [19], [20]. Hybrid switching [19] and buffered wormhole [20] remove a blocked packet to release held physical channels by using either the processing node memory [19] or a central buffer [20]. Layered switching divides a long packet into several groups and tries to keep SA grants for a whole group [13]. Our research is different; we focus on improving the performance while avoiding deadlock.

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