

# University of Toronto

## Term Test 2

Date - Mar 17, 2010

Duration: 1.5 hrs

ECE334 — Digital Electronics

Lecturer - D. Johns

**ANSWER QUESTIONS ON THESE SHEETS USING BACKS IF NECESSARY**

1. Equation sheet is on last page of test.
  2. Only tests written in pen will be considered for a re-mark.
  3. Calculator type unrestricted
  4. Grading indicated by [ ]. Attempt all questions since a blank answer will certainly get 0.
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**Last Name:** \_\_\_\_\_

**First Name:** \_\_\_\_\_

**Student #:** \_\_\_\_\_

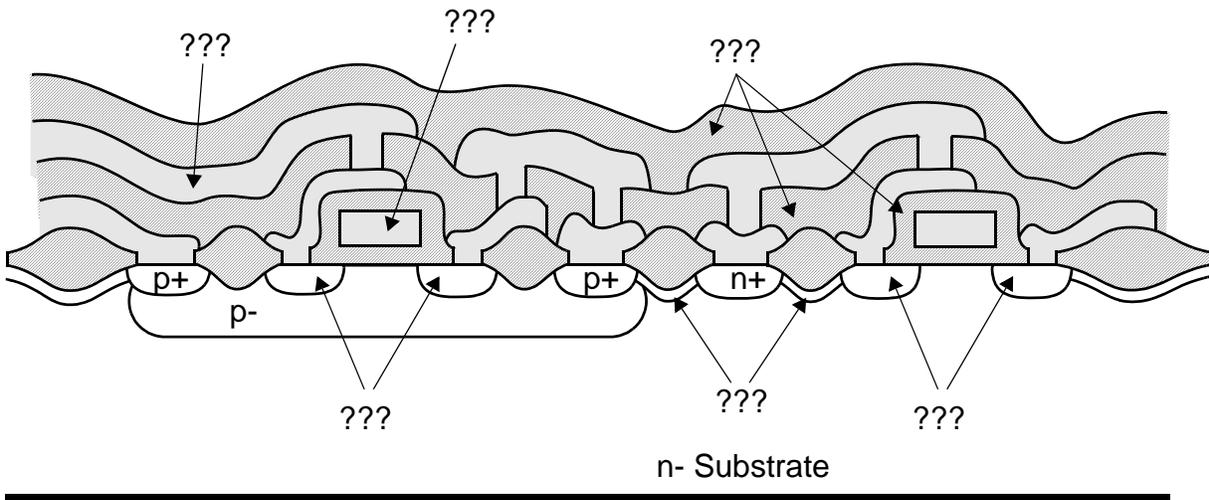
Question	Mark
1	
2	
3	
4	
5	
Total	

**(max grade = 29)**

[5] **Question 1:** Answer the True [T] or False [F] questions below by **circling** the correct answer. Each correct answer is worth 0.5 marks.

- T F When creating metal wires on a chip, first silicon dioxide is grown and photoresist is used to etch where wires should exist. Next, aluminum is sprayed on using silicon dioxide as a mask.
- T F When creating metal wires on a chip, first aluminum is sprayed on the entire micro-chip, then photoresist and silicon oxide is used to mask where wires should exist and the rest is etched off.
- T F In a self-aligned process, the drain/source junctions are first formed and then the gate is formed above the drain/source junctions so that it is self-aligned.
- T F The silicon dioxide layer formed under the gate region is grown using wet oxidation instead of dry oxidation.
- T F Tungsten is used in via and contact holes due to its low resistance.
- T F P-type silicon is made by doping pure silicon with boron.
- T F The dynamic power of a digital chip is due to the energy being dissipated across capacitors in the chip.
- T F In CMOS circuits, to keep all the drain/source diodes reverse biased, the substrate (or bulk) of all NMOS transistors should be tied to  $V_{dd}$  while the substrate (or bulk) of all PMOS transistors should be tied to ground.
- T F A pseudo-NMOS gate with power supplies 0 and  $V_{dd}$  has its output high level equal to  $V_{dd}$  while its output low level is a value greater than 0.
- T F  $V_{TH}$  for an inverter is defined to be the input voltage where the inverter's gain is largest.

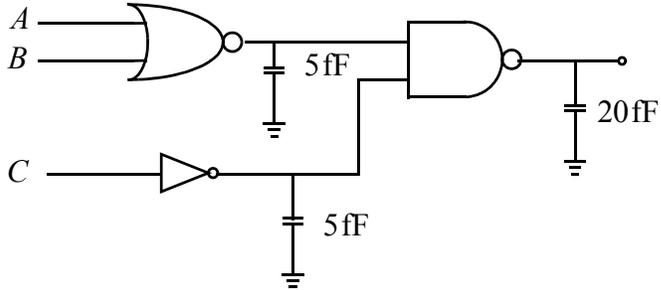
[6] Question 2: Consider the following cross-section of a p-well process (not n-well)



- a) On the above diagram, label all the “???” signs with the material name (i.e. polysilicon, silicon dioxide, metal, p+, n+, p-, n-, etc.).
- b) What is the purpose of the p+ in the p-well and the n+ in the n- substrate?
- c) What is the purpose of field-implants?
- d) Explain clearly why metal is not used as the gate material in a self-aligned process.

[6] **Question 3:** Find the dynamic power dissipation,  $P_{\text{dyn}}$ , for the following CMOS circuit assuming the clock is 1GHz,  $V_{\text{DD}} = 2.5\text{V}$  and the inputs have the following probability values that change on the rising edge of the clock.

$$P(A=1) = 0.5, P(B=1) = 0.4, P(C=1) = 0.7$$



$$P_{\text{dyn}} =$$

[6] **Question 4:** Consider a metal 1 (first layer of metal) aluminum wire that is  $0.8\mu\text{m}$  above the substrate, is  $0.5\mu\text{m}$  in height and has a width of  $0.25\mu\text{m}$  and has a length of  $5\text{ mm}$ . Recall that the resistivity of aluminum is  $2.8\mu\Omega \cdot \text{cm}$

a) Find the resistance per  $\mu\text{m}$ ,  $R_w$ , and the capacitance per  $\mu\text{m}$ ,  $C_w$ .

$$R_w =$$

$$C_w =$$

a) Estimate the delay,  $t_d$ , of this wire assuming the delay is  $1.2\tau$ .

$$t_d =$$

b) Estimate the delay of this wire if the width is increased to  $1\mu\text{m}$  and other parameters are unchanged.

$$t_d =$$

[6] **Question 5:** It is desired to drive a 1pF capacitive load given that a minimum size inverter has a gate capacitance of 4fF and its inherent delay is 15ps.

a) Find the delay if a single inverter is used.

b) Find the delay if an inverter chain is used where a fanout factor of 4 is used for inverter sizing.

c) Explain why a fanout factor of 4 is generally used for inverter sizing in an inverter chain instead of a factor of  $e$  which was derived in class to be optimum. (hint: what was overlooked in the class derivation?)

**Constants:**  $k = 1.38 \times 10^{-23} \text{ JK}^{-1}$ ;  $q = 1.602 \times 10^{-19} \text{ C}$ ;  $V_T = kT/q \approx 26 \text{ mV}$  at  $300 \text{ }^\circ\text{K}$ ;

$$\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m}; k_{\text{ox}} = 3.9; \text{caps: } C_{\text{ox}} = (k_{\text{ox}}\epsilon_0)/t_{\text{ox}}; C_j = C_{j0}/(1 + V_R/\phi_0)^{M_j};$$

**NMOS:**  $\beta_n = \mu_n C_{\text{ox}}(W/L)$ ;  $V_{in} > 0$ ;  $V_{DS} \geq 0$ ; (triode)  $I_D = \beta_n((V_{GS} - V_{in})V_{DS} - (V_{DS}^2/2))$ ; (active)  $I_D = 0.5\beta_n(V_{GS} - V_{in})^2$ ;

$$\text{(triode) } V_{DS} \leq (V_{GS} - V_{in}); \text{(active) } V_{DS} \geq (V_{GS} - V_{in}); V_{in} = V_{in0} + \gamma(\sqrt{V_{SB} + \phi_s} - \sqrt{\phi_s});$$

$$\text{(subthreshold) } I_D = I_{D0} e^{((V_{GS} - V_{in})/(nV_T))} (1 - e^{-V_{DS}/V_T});$$

**PMOS:**  $\beta_p = \mu_p C_{\text{ox}}(W/L)$ ;  $V_{ip} < 0$ ;  $V_{DS} \leq 0$ ; (triode)  $I_D = \beta_p((V_{GS} - V_{ip})V_{DS} - (V_{DS}^2/2))$ ; (active)  $I_D = 0.5\beta_p(V_{GS} - V_{ip})^2$ ;

$$\text{(triode) } V_{DS} \geq (V_{GS} - V_{ip}); \text{(active) } V_{DS} \leq (V_{GS} - V_{ip});$$

**Simple cap model:**  $C_g = C_{\text{ox}}WL$ ; if  $L_{\text{min}}$ :  $C_{gu} \equiv C_{\text{ox}}L_{\text{min}}$ ;  $C_g = C_{gu}W$ ;  $C_d = C_s = C_{du}W$ ;

**CMOS inverter:**  $V_{TH} = (V_{DD} + V_{tp} + V_{in}r)/(1 + r)$ ;  $r = \sqrt{(\mu_n(W/L)_n)/(\mu_p(W/L)_p)}$ ;

**RC delay est:**  $t_{dr} = t_{df} = 1.2\tau$ ;  $\tau = R_{\text{eq}}C$ ;  $R_{\text{eqn}} = 2.5/(\mu_n C_{\text{ox}}(W/L)_n(V_{DD} - V_{in}))$ ;  $R_{\text{eqp}} = 2.5/(\mu_p C_{\text{ox}}(W/L)_p(V_{DD} + V_{ip}))$ ;

$$(W_p/W_n)_{\text{opt}} = \sqrt{\mu_n/\mu_p} \quad \text{Unit delay est: } t_{df2}/t_{df1} = (C_{L2}/C_{L1}) \times ((W/L)_{n1}/(W/L)_{n2})$$

**Min delay:**  $t_{\text{delay}} = \tau_{\text{inv}}(C_{\text{out}}/C_{\text{in}})$ ;  $\text{total}_{\text{delay}} = Nf\tau_{\text{inv}}$ ;  $f^N = C_{\text{out}}/C_{\text{in}}$ ; usually  $f = 4$

**Power diss:**  $P_{\text{dyn}} = P_{1 \rightarrow 0}fC_LV_{DD}^2$ ;  $P_{\text{dp}} = 0.5P_{1 \rightarrow 0}fV_{DD}I_{\text{peak}}(t_r + t_f)$ ;  $I_{\text{peak}} = 0.5\beta_n(V_{TH} - V_{in})^2$ ;

**Elmore Delay:**  $\tau_i \equiv \sum C_k R_{ik}$ ; dist RC,  $\tau \equiv RC/2$ ;

**Interconnect:**  $R = (\rho l)/(tw)$ ;  $R_{\square} = \rho/t$ ;  $C = (\epsilon_{\text{ox}}wl)/t$ ;  $C = \epsilon_{\text{ox}}l(w/h + 0.77 + 1.06(w/h)^{0.25} + 1.06(t/h)^{0.5})$ ;