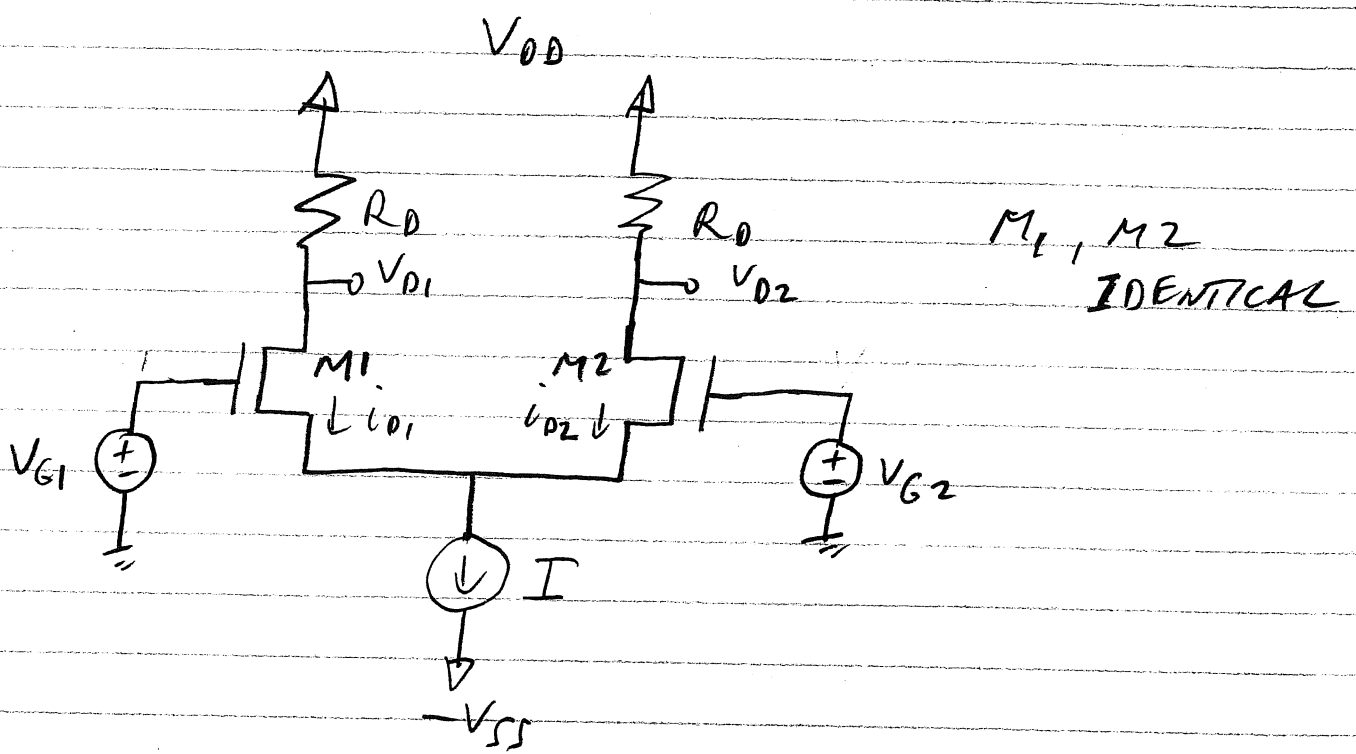


MD1

MOS DIFFERENTIAL PAIR



$$i_{D1} + i_{D2} = I \quad \text{IF } M_1, M_2 \text{ ACTIVE}$$

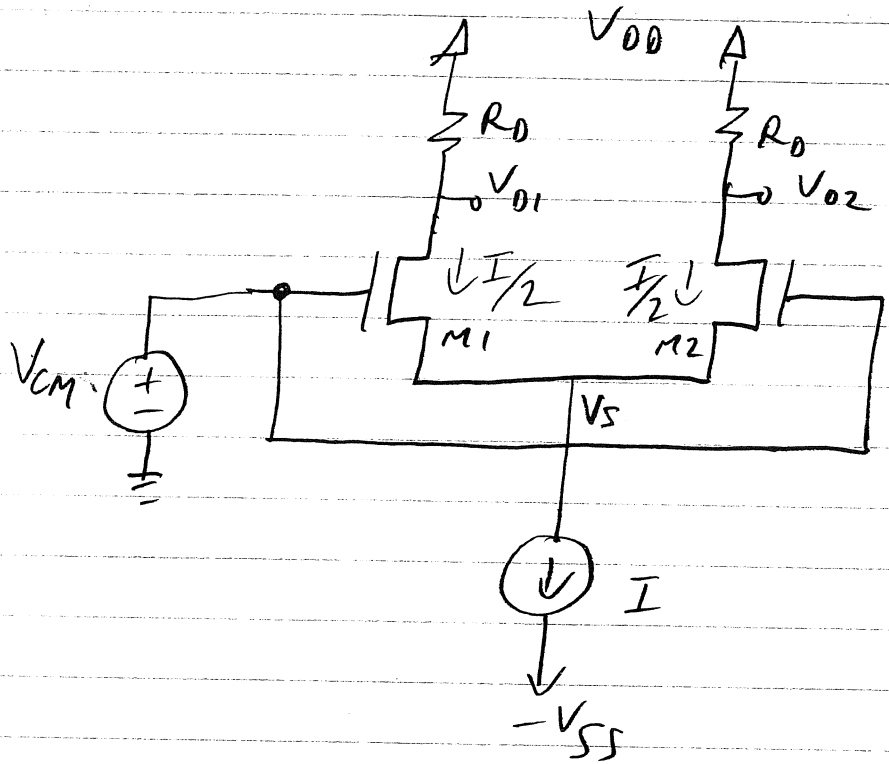
$$\text{IF } V_{G1} = V_{G2} \Rightarrow i_{D1} = i_{D2} = \frac{I}{2}$$

$$\text{IF } V_{G1} > V_{G2} \Rightarrow i_{D1} > i_{D2}$$

$$V_{G1} < V_{G2} \Rightarrow i_{D1} < i_{D2}$$

CAN "STEER" CURRENT I

COMMON-MODE INPUT OPERATION



$V_{01} = V_{02} = V_{DD} - \frac{I}{2} R_0$ WHILE M_1, M_2 ACTIVE

$I_{D1} = \frac{I}{2} = \frac{\mu_n C_{ox}}{2} \left(\frac{W}{L}\right) (V_{OV})^2$

$V_{OV(\frac{I}{2})} = \sqrt{\frac{I}{\mu_n C_{ox} (\frac{W}{L})}}$

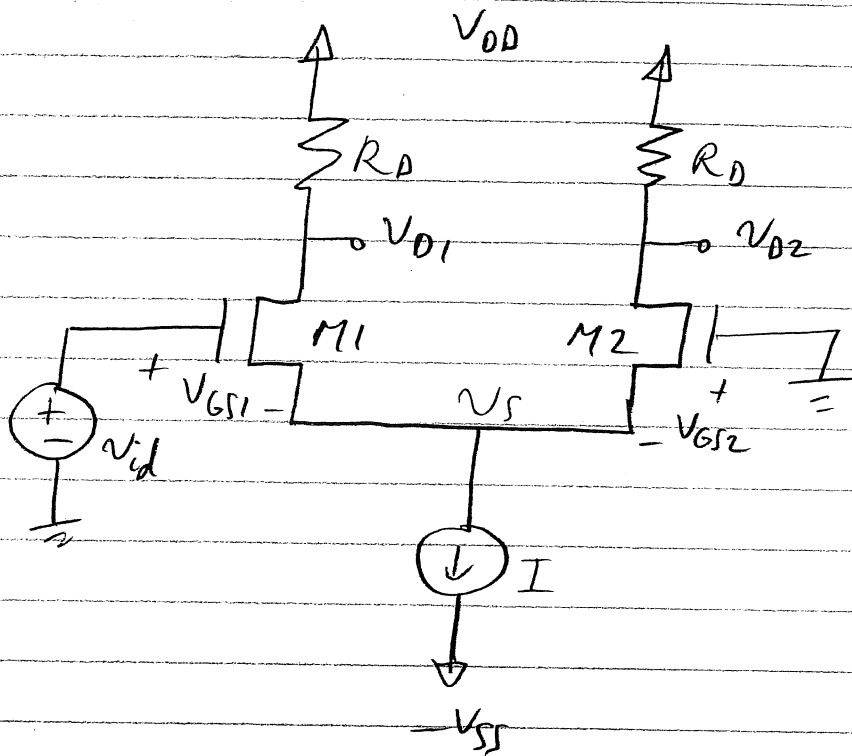
$V_{CM-MAX} = V_t + V_{DD} - \frac{I}{2} R_0$ (ONE V_t ABOVE V_{01})

$V_{CM-MIN} = -V_{SS} + V_{CS} + V_t + V_{OV(\frac{I}{2})}$

(V_{CS} IS VOLTAGE NEEDED ACROSS I CURRENT SOURCE)

M.D.3

LARGE SIGNAL WITH DIFFERENTIAL VOLTAGE



IF $V_{id} \gg 0$ ALL I FLOWS THROUGH M_1

$V_{id} \ll 0$ " " " " M_2

WHEN $i_{D2} \approx 0$ (M_2 JUST TURNS OFF)

$$V_{GS2} = V_{th} \Rightarrow V_S = -V_{th}$$

$$V_{GS1} = V_{th} + V_{OV(I)} \text{ WHERE}$$

$$V_{OV(I)} = \sqrt{2I / (\mu_n C_{ox} (W/L))}$$

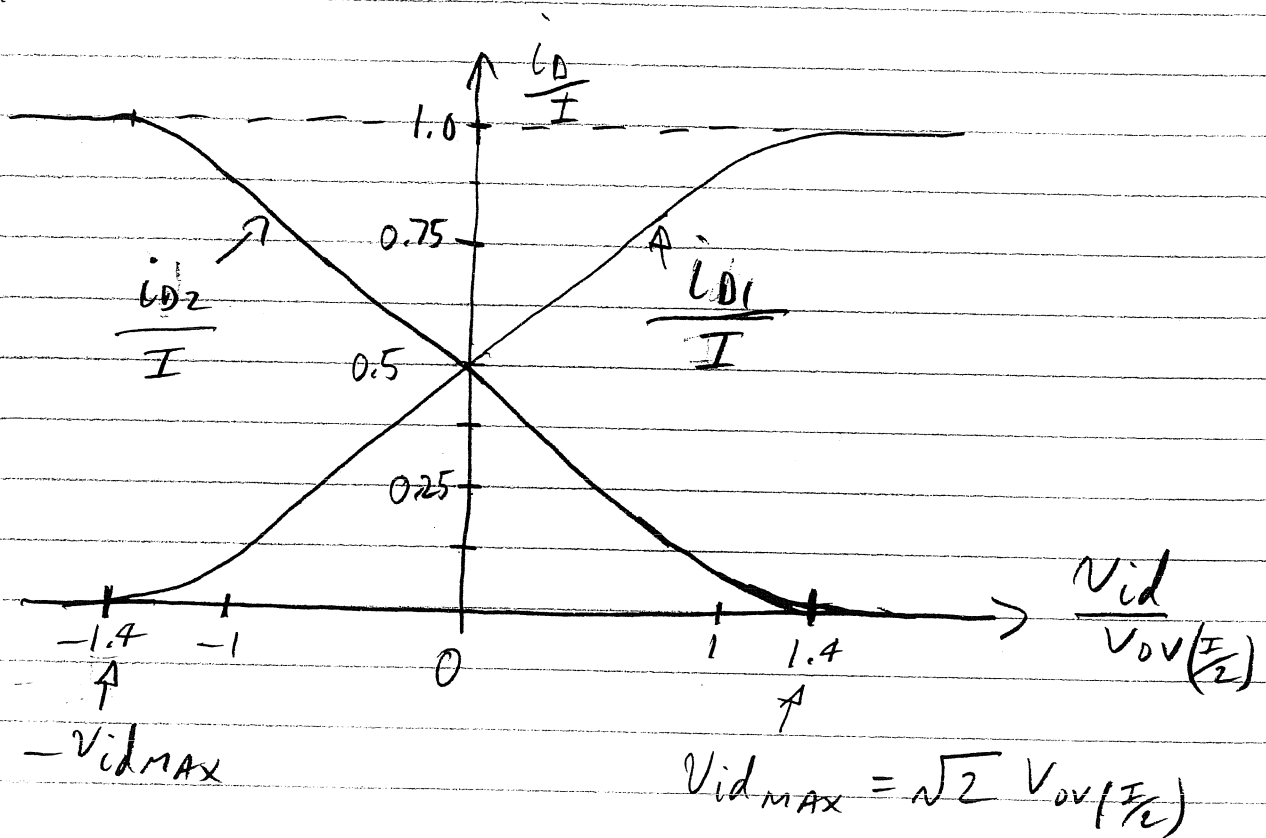
$$= \sqrt{2} V_{OV(I/2)}$$

MDA

$$\begin{aligned} \text{SINCE } v_{id} &= v_s + v_{GS1} \\ &= -v_{tn} + v_{tn} + \sqrt{v_{OV1}} \end{aligned}$$

$$v_{id \text{ MAX}} = \sqrt{2} v_{OV} \left(\frac{I}{2} \right)$$

WHERE CURRENT CAN BE STEERED TO M_1 OR M_2



CAN SHOW

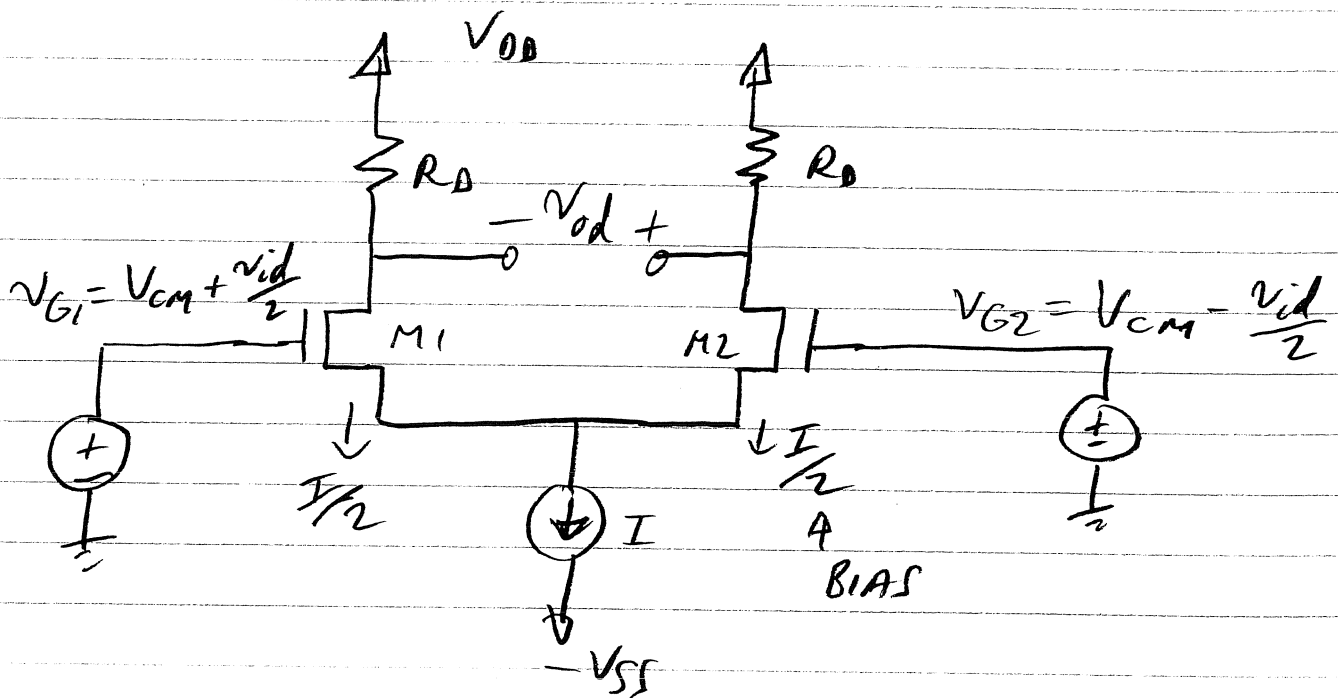
$$i_{D1} = \frac{I}{2} + \left(\frac{I}{v_{OV} \left(\frac{I}{2} \right)} \right) \left(\frac{v_{id}}{2} \right) \left(\sqrt{1 - \left(\frac{v_{id}/2}{v_{OV} \left(\frac{I}{2} \right)} \right)^2} \right)$$

i_{D2} SIMILAR EQN.

MDS

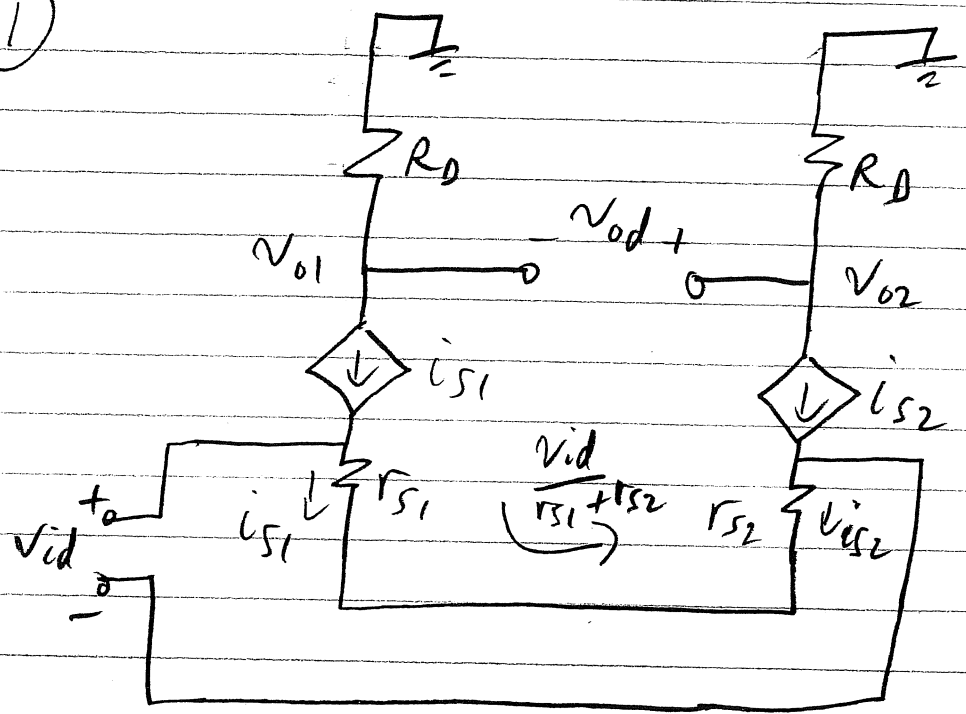
- i_D IS APPROX LINEAR RELATIONSHIP TO v_{id} NEAR $v_{id} \cong 0$
- MORE NON-LINEAR AS v_{id} INCREASES.

SMALL-SIGNAL OPERATION



2 WAYS TO LOOK AT CIRCUIT. FOR SMALL-SIGNAL ANALYSIS

①



$$i_{S1} = \frac{v_{id}}{r_{S1} + r_{S2}} = \frac{v_{id}}{2 r_S}$$

ASSUME
 $r_S = r_{S1} = r_{S2}$

$$v_{01} = -i_{S1} R_D \quad \& \quad i_{S2} = -i_{S1}$$

$$v_{02} = -i_{S2} R_D = i_{S1} R_D$$

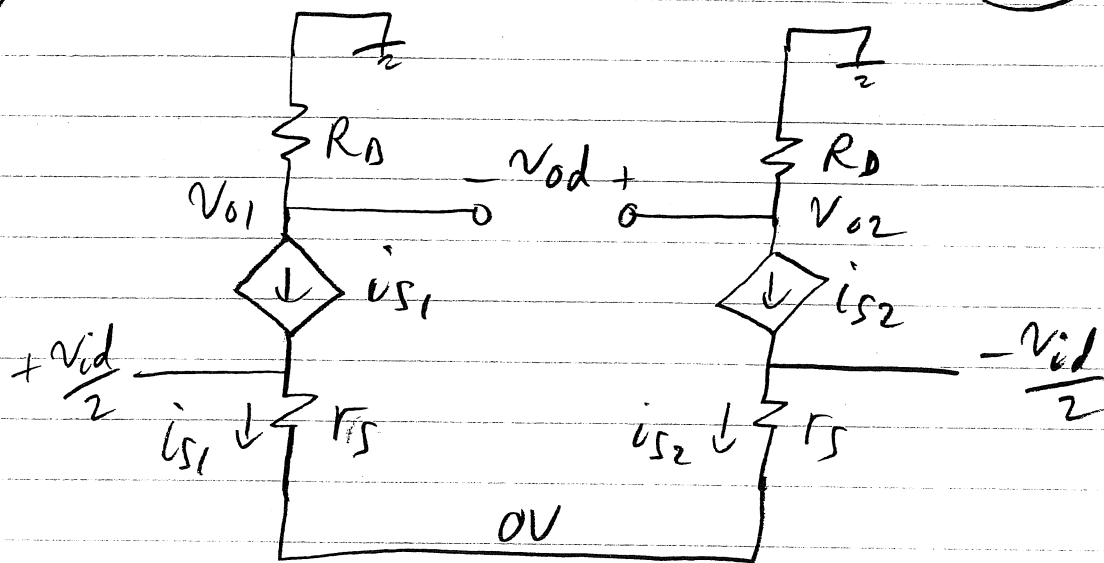
$$v_{0d} = v_{02} - v_{01} = 2 i_{S1} R_D = \frac{R_D}{r_S} v_{id}$$

$$\frac{v_{0d}}{v_{id}} = \frac{R_D}{r_S} = g_m R_D$$

2

BALANCED VIEW

1707



↑
SINCE BALANCED
CIRCUIT.

$$V_{01} = - \left(\frac{R_D}{r_S} \right) \left(\frac{V_{id}}{2} \right)$$

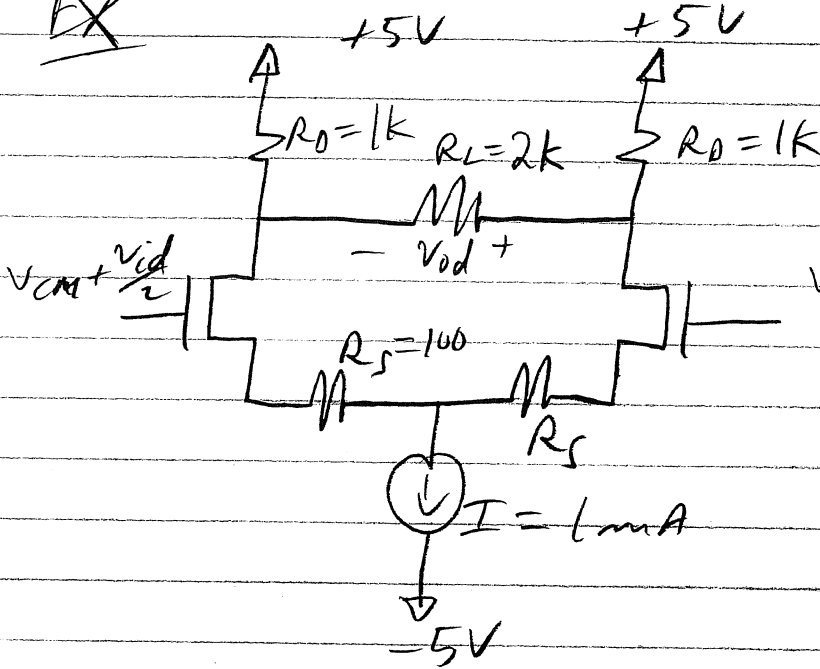
$$V_{02} = - \left(\frac{R_D}{r_S} \right) \left(- \frac{V_{id}}{2} \right)$$

$$V_{0d} = V_{02} - V_{01} = \left(\frac{R_D}{r_S} \right) V_{id} = g_m R_D V_{id}$$

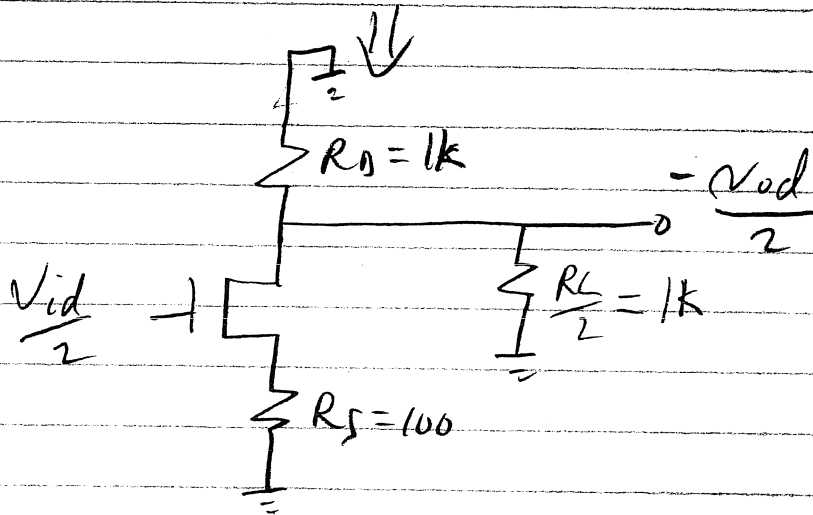
DIFFERENTIAL HALF CIRCUIT.

IF CIRCUIT IS BALANCED \Rightarrow DO ANALYSIS ON HALF CIRCUIT

EX



ASSUME $V_{OV} = V_{OV}(\frac{I}{2}) = 0.2V$
 $\lambda = 0$



$$g_m = \frac{1}{r_s} = \frac{2I_D}{V_{OV}} = \frac{2(I/2)}{V_{OV}} = \frac{2(0.5)}{0.2} = 5 \text{ mA/V}$$

$$r_s = 200 \Omega$$

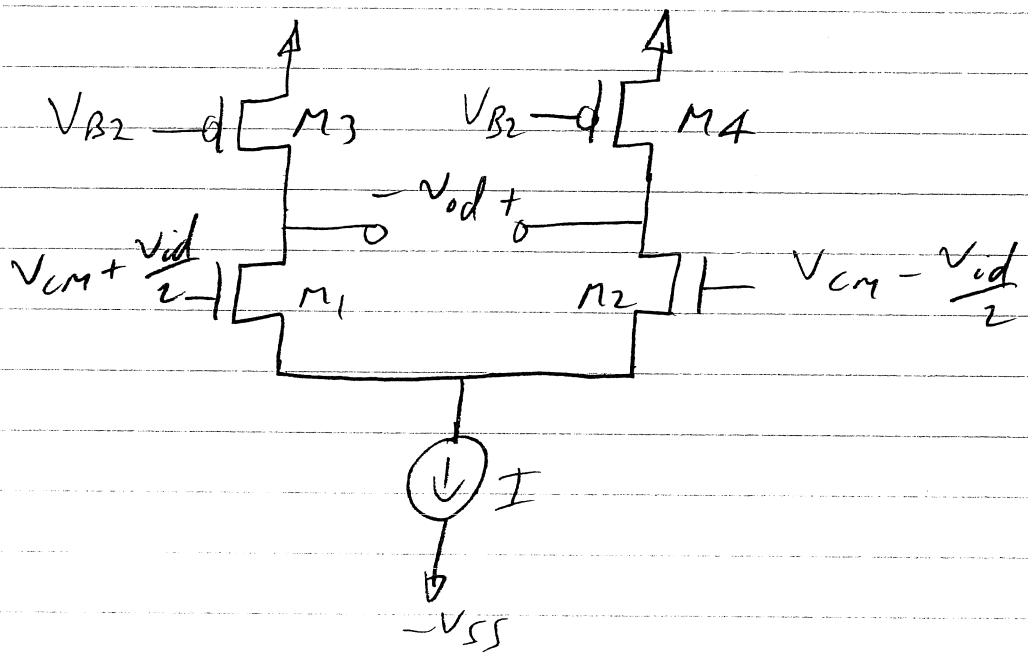
M7D9

$$\frac{-\frac{v_{od}}{2}}{\frac{v_{id}}{2}} = \frac{-v_{od}}{v_{id}} = \frac{-[R_D || (\frac{R_L}{2})]}{r_s + R_s}$$

$$-\frac{v_{od}}{v_{id}} = \frac{-500}{300} = -1.67 \frac{V}{V}$$

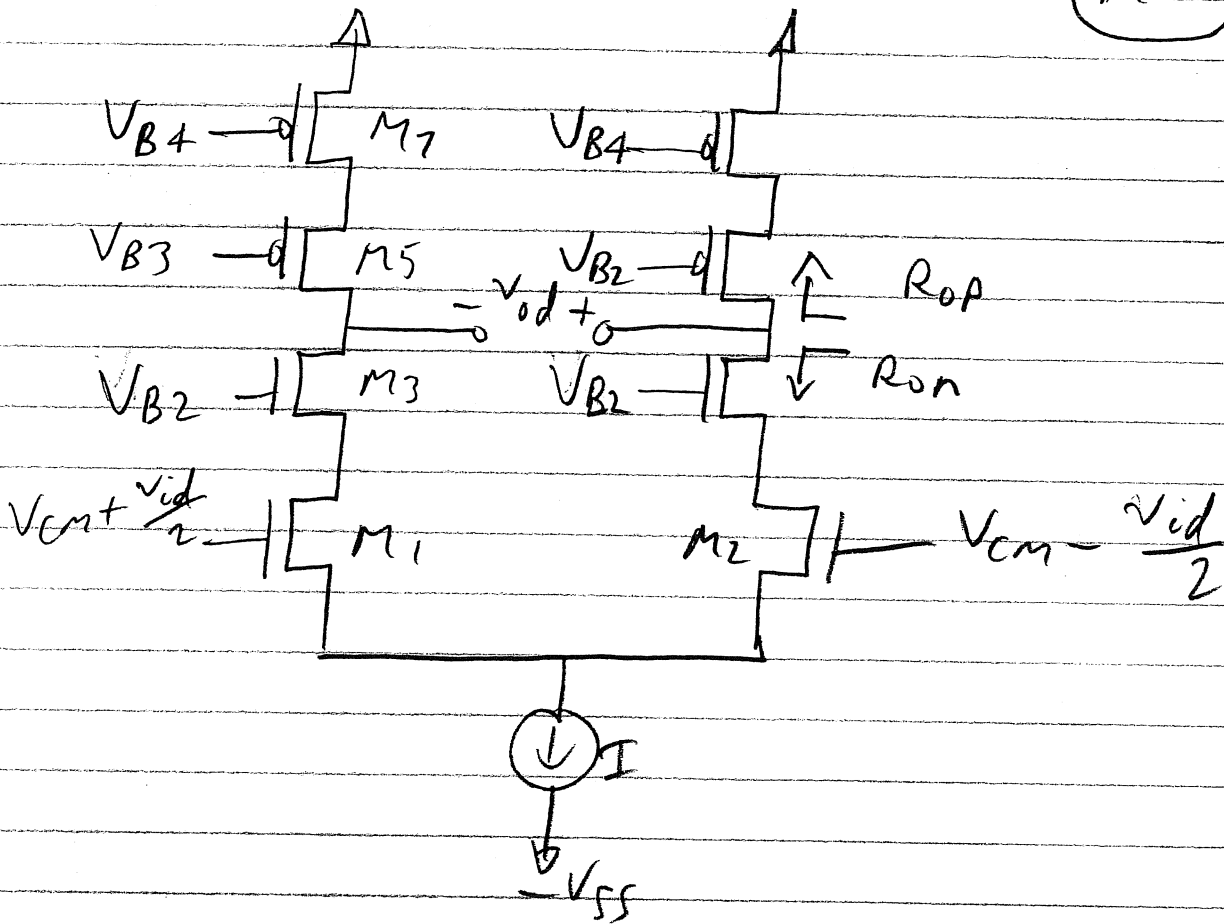
$$\frac{v_{od}}{v_{id}} = 1.67 \frac{V}{V}$$

DIFF PAIR WITH CURRENT SOURCE LOADS



$$A_d = \frac{v_{od}}{v_{id}} = g_{m1} (r_{o1} || r_{o3})$$

MD10



$$A_d = \frac{v_{od}}{v_{id}} = g_{m1} (R_{on} \parallel R_{op})$$

$$R_{on} \cong (g_{m3} r_{o3}) r_{o1}$$

$$R_{op} \cong (g_{m5} r_{o5}) r_{o7}$$

DIFFERENTIAL & COMMON-MODE SIGNALS

- MANY CIRCUITS RELY ON DIFFERENTIAL SIGNALS AS THEIR SIGNALS AND TRY TO IGNORE (OR REJECT) COMMON-MODE SIGNALS

- ETHERNET

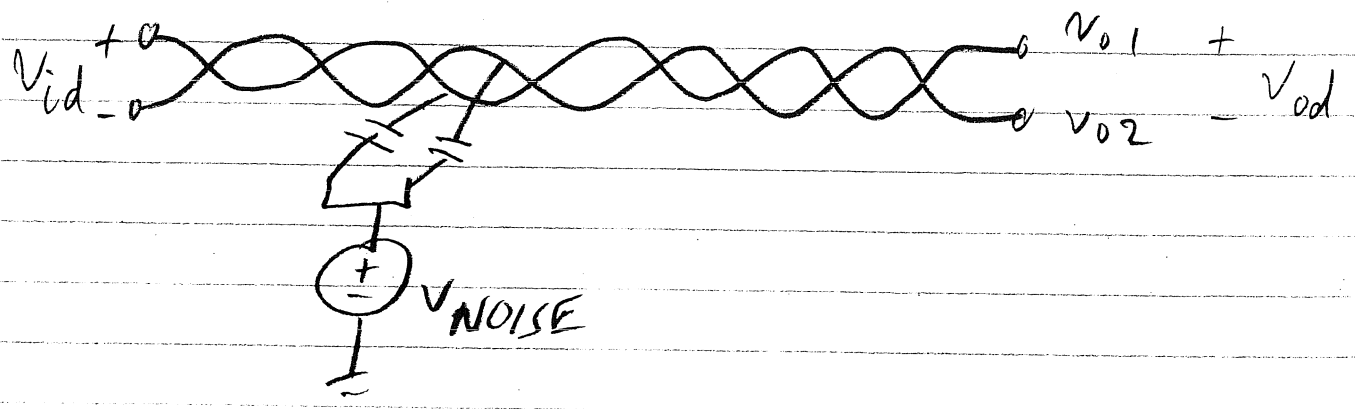
TWISTED WIRE PAIR



TRANSMIT & RECEIVE DIFF SIGNALS

SO COMMON MODE INTERFERENCE CAN BE REJECTED

- TWISTED PAIR HELPS BUT COMMON-MODE SIGNAL STILL GETS THROUGH.

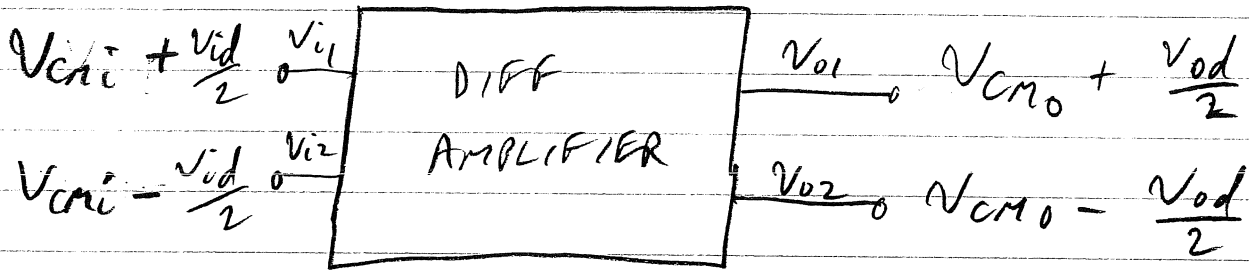


$$V_{o1} = \frac{V_{id}}{2} + V_{NOISE}$$

$$V_{o2} = -\frac{V_{id}}{2} + V_{NOISE}$$

$$V_{od} = V_{o1} - V_{o2} = V_{id}$$

DIFF AMP



$$V_{id} \equiv V_{i1} - V_{i2}$$

$$V_{cmi} \equiv \frac{V_{i1} + V_{i2}}{2}$$

$$V_{od} \equiv V_{o1} - V_{o2}$$

$$V_{cmo} \equiv \frac{V_{o1} + V_{o2}}{2}$$

DEFINE A GAINS THROUGH AMP

(M13)

$$A_d \equiv \frac{V_{od}}{V_{id}} \quad \text{DIFFERENTIAL GAIN}$$

$$A_{cm-cm} \equiv \frac{V_{cmo}}{V_{cmi}} \quad \text{COMMON MODE TO COMMON MODE GAIN}$$

$$A_{cm} = \frac{V_{od}}{V_{cmi}} \quad \text{COMMON MODE TO DIFFERENTIAL GAIN}$$

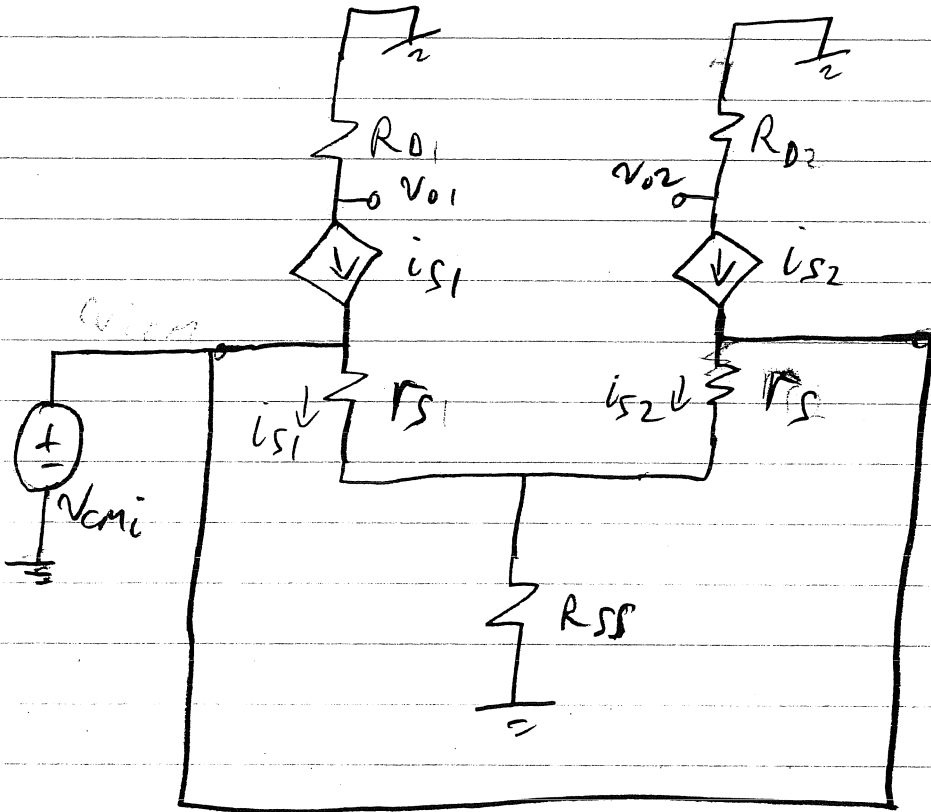
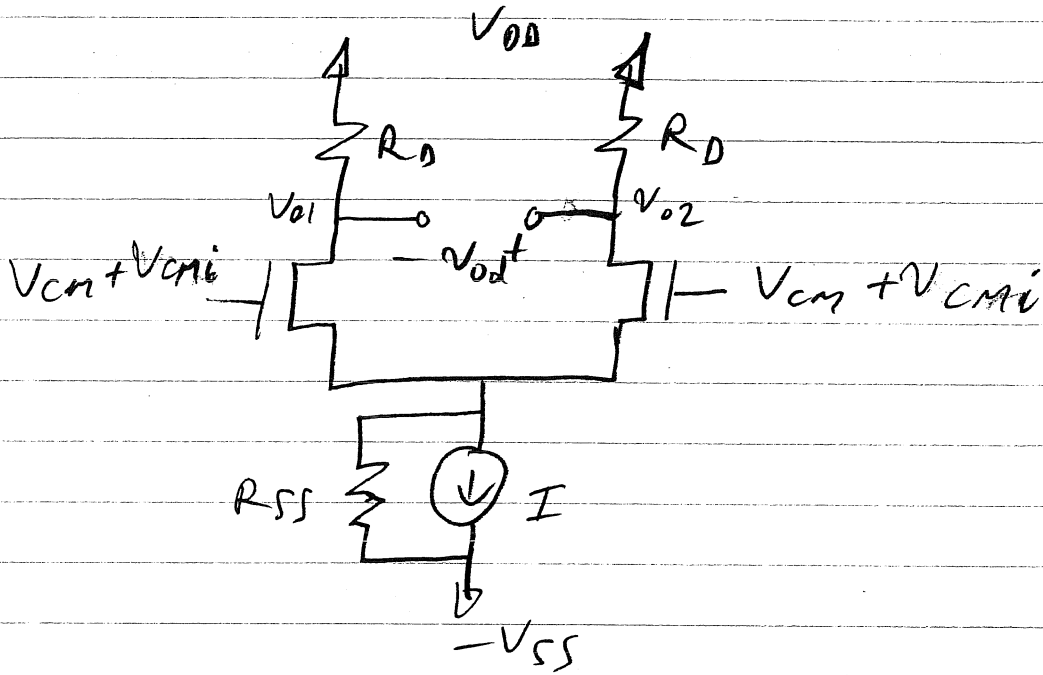
$$A_{d-cm} \equiv \frac{V_{cmo}}{V_{id}} \quad \text{DIFF TO CM GAIN (USUALLY UNIMPORTANT)}$$

A_{cm-cm} KEEP SMALL SO COMMON-MODE SIGNALS DO NOT AMPLIFY (< 1)

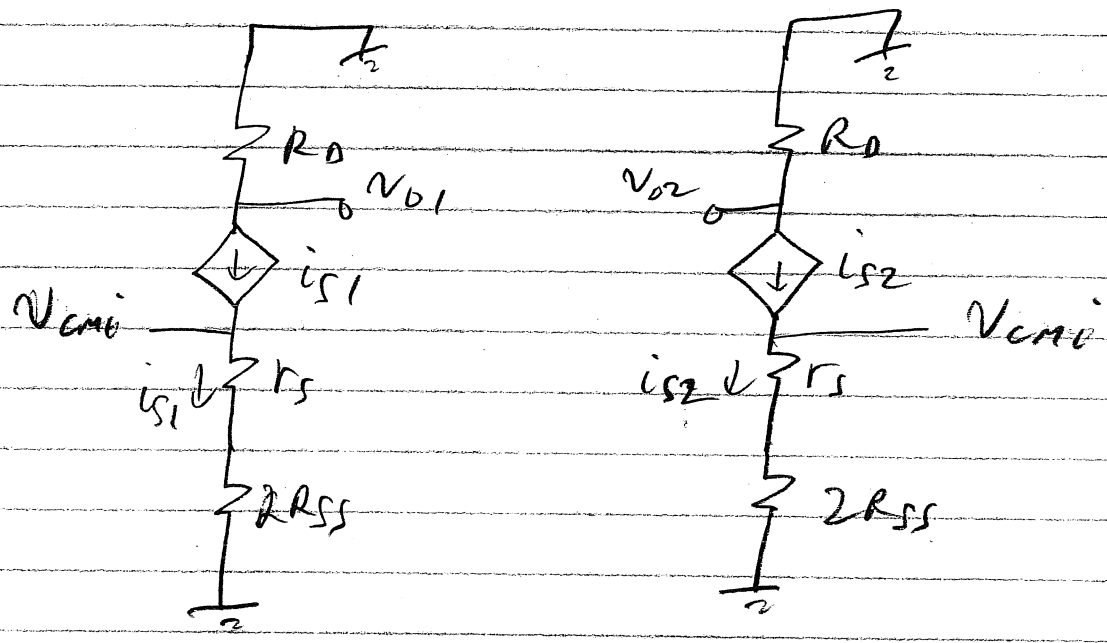
MOST IMPORTANT ARE A_d & A_{cm}
 \downarrow WANT $A_d \gg A_{cm}$ SO

CM SIGNALS ARE REJECTED.

Ad-cm



EQUIV TO HALF CIRCUITS



$$\frac{V_{o1}}{V_{CM}} = - \frac{R_D}{r_s + 2R_{SS}} = \frac{V_{o2}}{V_{CM}}$$

SO $V_{od} = V_{o1} - V_{o2} = 0$ & $A_{CM} = 0$

IF PERFECTLY MATCHED.

IF RESISTORS MISMATCHED BY ΔR_D

$$R_{D1} = R_D \quad \& \quad R_{D2} = R_D + \Delta R_D$$

CAN SHOW $A_{CM} = - \left(\frac{R_D}{2R_{SS}} \right) \left(\frac{\Delta R_D}{R_D} \right)$

IF TRANSISTORS g_m MISMATCHED BY $\frac{\Delta g_m}{g_m}$

CAN SHOW

$$A_{cm} \approx \left(\frac{R_D}{2R_{SS}} \right) \left(\frac{\Delta g_m}{g_m} \right)$$

CMRR COMMON-MODE REJECTION RATIO

USUALLY CARE ABOUT RATIO $\frac{A_d}{A_{cm}}$

SO DEFINE

$$CMRR \equiv \frac{|A_d|}{|A_{cm}|}$$

OR IN dB

$$CMRR (dB) = 20 \log \frac{|A_d|}{|A_{cm}|}$$

SINCE $A_d = g_m R_D$

THEN FOR $\Delta R \Rightarrow CMRR = \frac{2g_m R_{SS}}{(\Delta R/R_D)}$

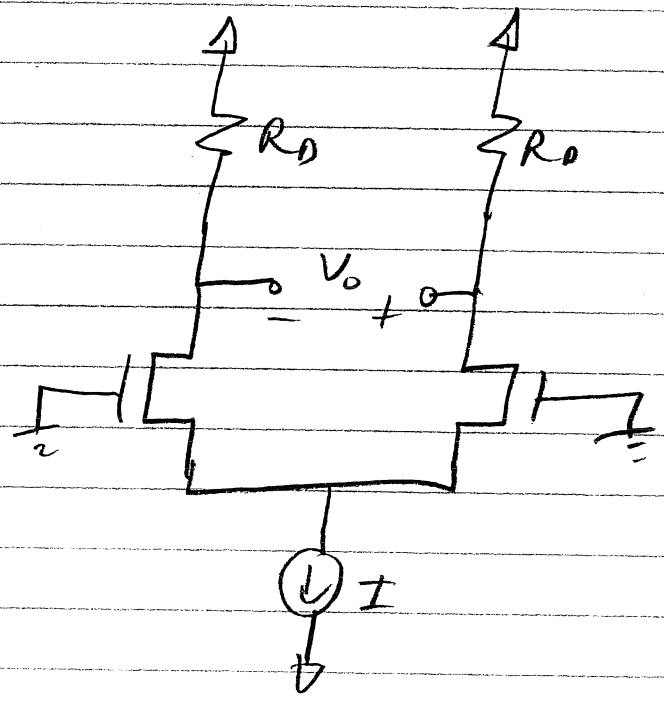
FOR $\Delta g_m \Rightarrow CMRR = \frac{2g_m R_{SS}}{(\Delta g_m/g_m)}$

INPUT OFFSET OF DIFF PAIR (DC VALUE)

DEFINE V_{os} AS INPUT OFFSET VOLTAGE
NEEDED TO SET OUTPUT OFFSET TO ZERO

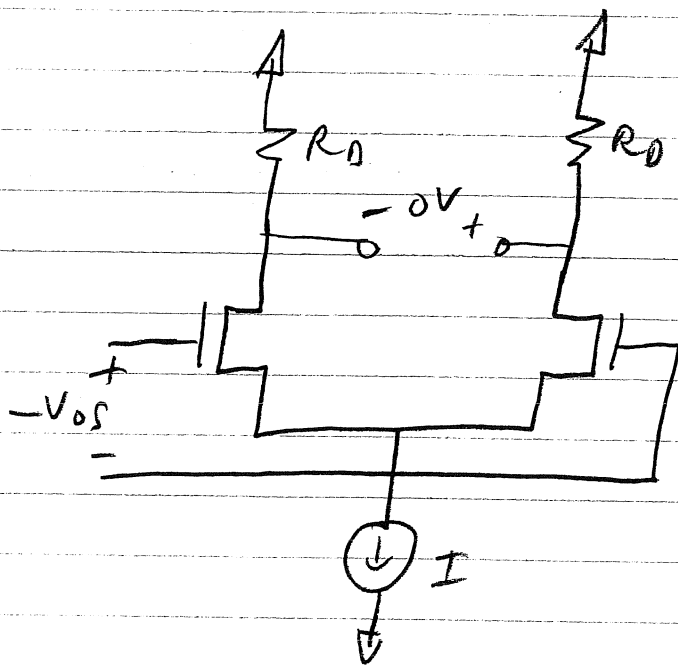
V_{os} INPUT OFFSET
 V_o OUTPUT OFFSET

$$V_{os} = \frac{V_o}{A_d}$$



IF $V_{id} = 0$
 V_o IS OUTPUT
OFFSET
VOLTAGE

M118



APPLY V_{OS} TO
SET $V_o = 0$

OFFSETS DUE TO R_D , (W/L) , V_{th} MISMATCH

TYPICALLY V_{th} DOMINATES

$$\text{or } V_{OS} = \Delta V_{th}$$

TYPICALLY $\Delta V_{th} \approx 1 \rightarrow 10 \text{ mV}$

FOR ΔR_D

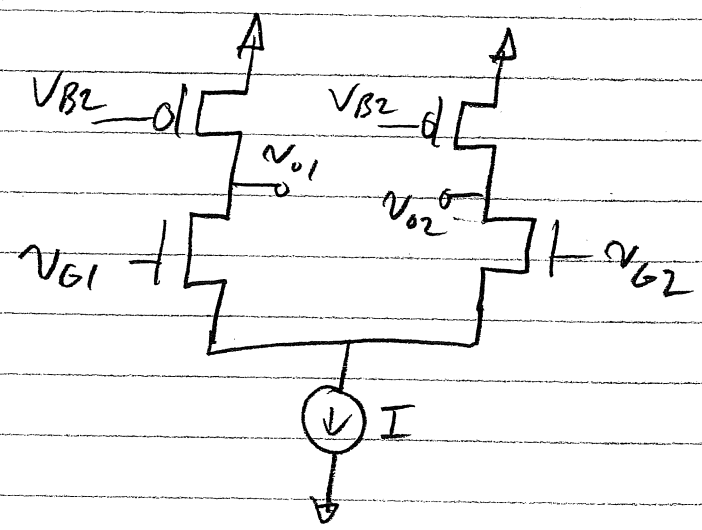
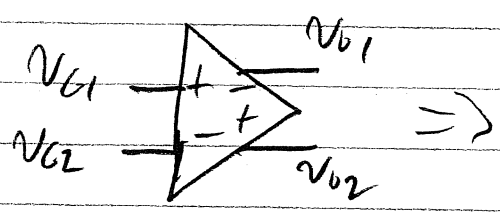
$$V_{OS} = \left(\frac{V_{OV}}{2}\right) \left(\frac{\Delta R_D}{R_D}\right)$$

FOR $\Delta (W/L)$

$$V_{OS} = \left(\frac{V_{OV}}{2}\right) \frac{\Delta (W/L)}{(W/L)}$$

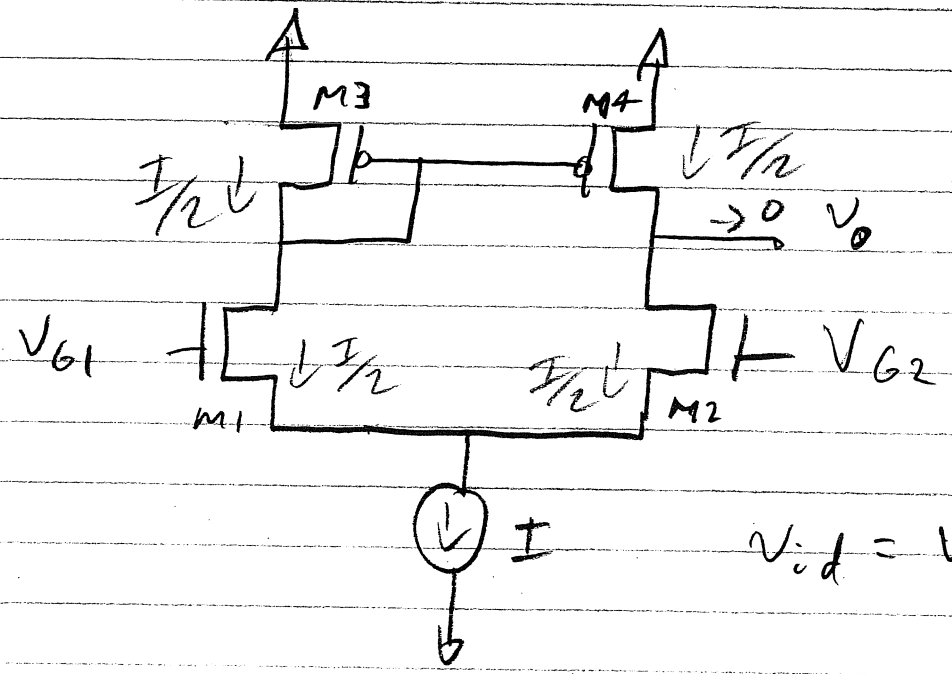
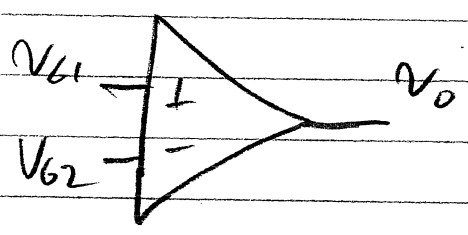
ACTIVE LOADS

MD19



FULLY DIFF

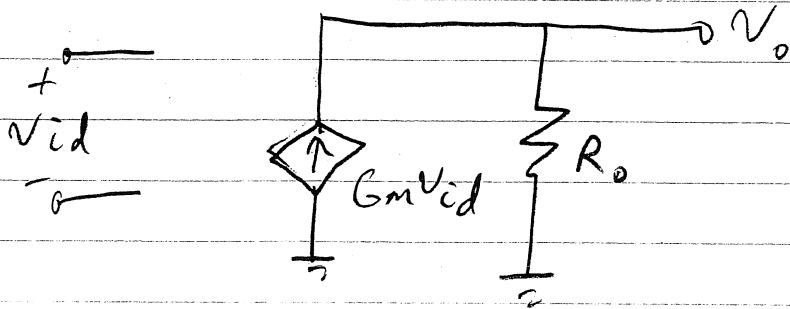
DIFF - SINGLE - ENDED



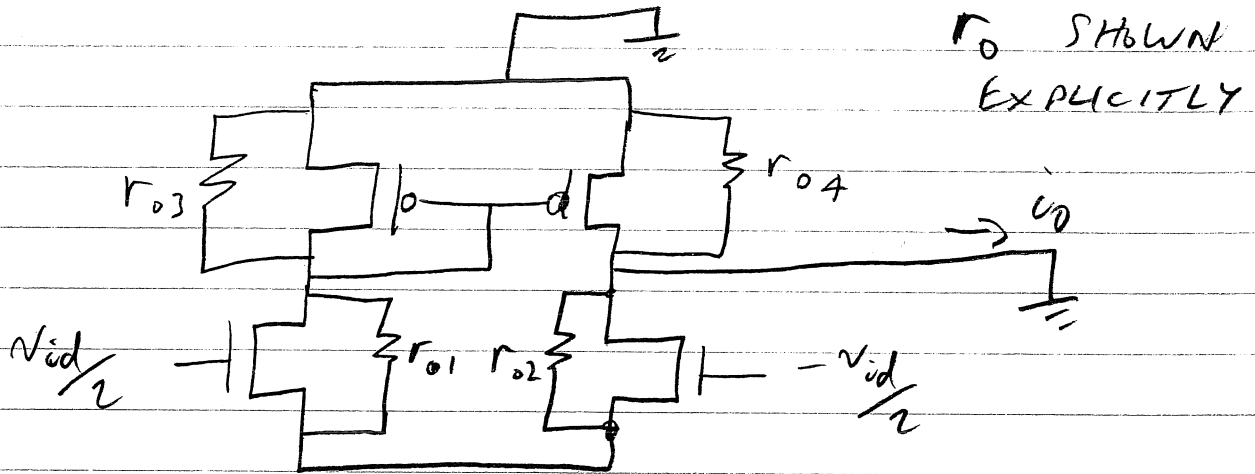
$$v_{id} = V_{G1} - V_{G2}$$

MD20

WANT TO MODEL ABOVE AS



TO FIND G_m

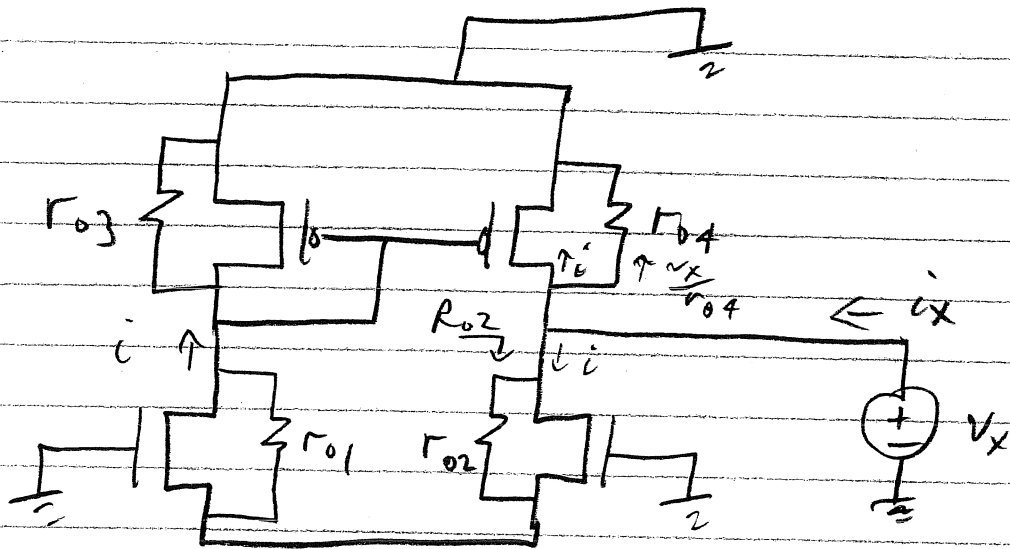


$$G_m \equiv \frac{i_o}{V_{id}} \quad \text{OR} \quad i_o = G_m V_{id}$$

CAN SHOW $G_m \approx g_m$ SEE
TEXT

WHERE $g_m = g_{m1} = g_{m2}$

TO FIND R_o



$$R_o \equiv \frac{V_x}{i_x}$$

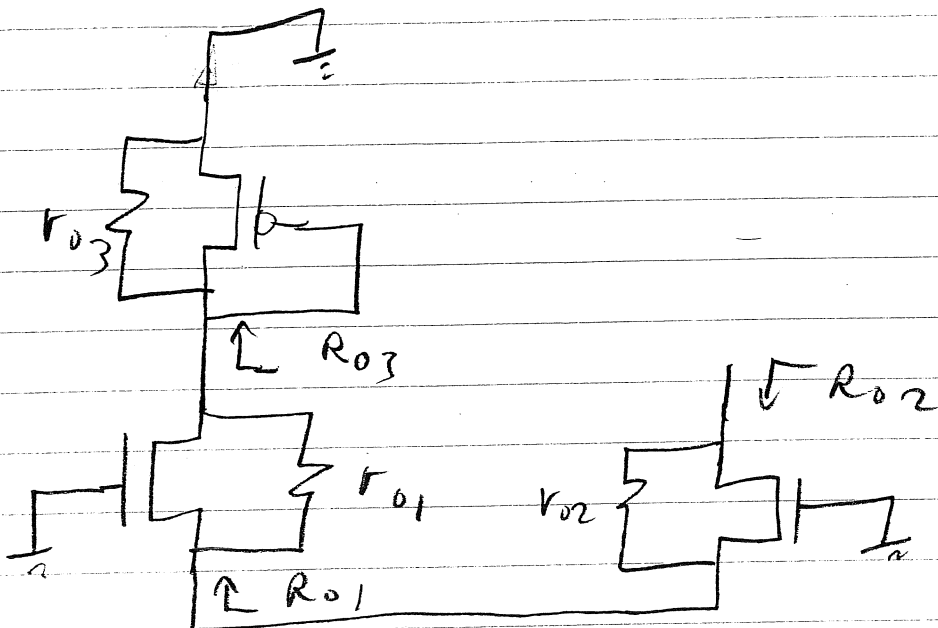
CAN SHOW $R_o \approx r_{o2} \parallel r_{o4}$

$$R_{o2} \approx 2r_{o2} \Rightarrow i \equiv \frac{V_x}{2r_{o2}}$$

$$i_x = i + i + \frac{V_x}{r_{o4}} = \frac{2V_x}{2r_{o2}} + \frac{V_x}{r_{o4}}$$

$$i_x = \frac{V_x}{r_{o2}} + \frac{V_x}{r_{o4}} \Rightarrow R_o = \frac{V_x}{i_x} = r_{o2} \parallel r_{o4}$$

MD21A



$$R_{o3} = \frac{1}{g_{m3}} \parallel r_{o3} \approx \frac{1}{g_{m3}}$$

$$R_{o1} = \frac{1}{g_{m1}} + \frac{R_{o3}}{g_{m1} r_{o1}} = \frac{1}{g_{m1}} + \frac{1}{g_{m1} g_{m3} r_{o1}}$$

$$R_{o1} \approx \frac{1}{g_{m1}}$$

$$R_{o2} \approx [1 + g_{m2} (R_{o1})] r_{o2} \quad g_{m1} = g_{m2}$$

$$= \left[1 + (g_{m2}) \left(\frac{1}{g_{m1}} \right) \right] r_{o2}$$

$$= \underline{\underline{2 r_{o2}}}$$

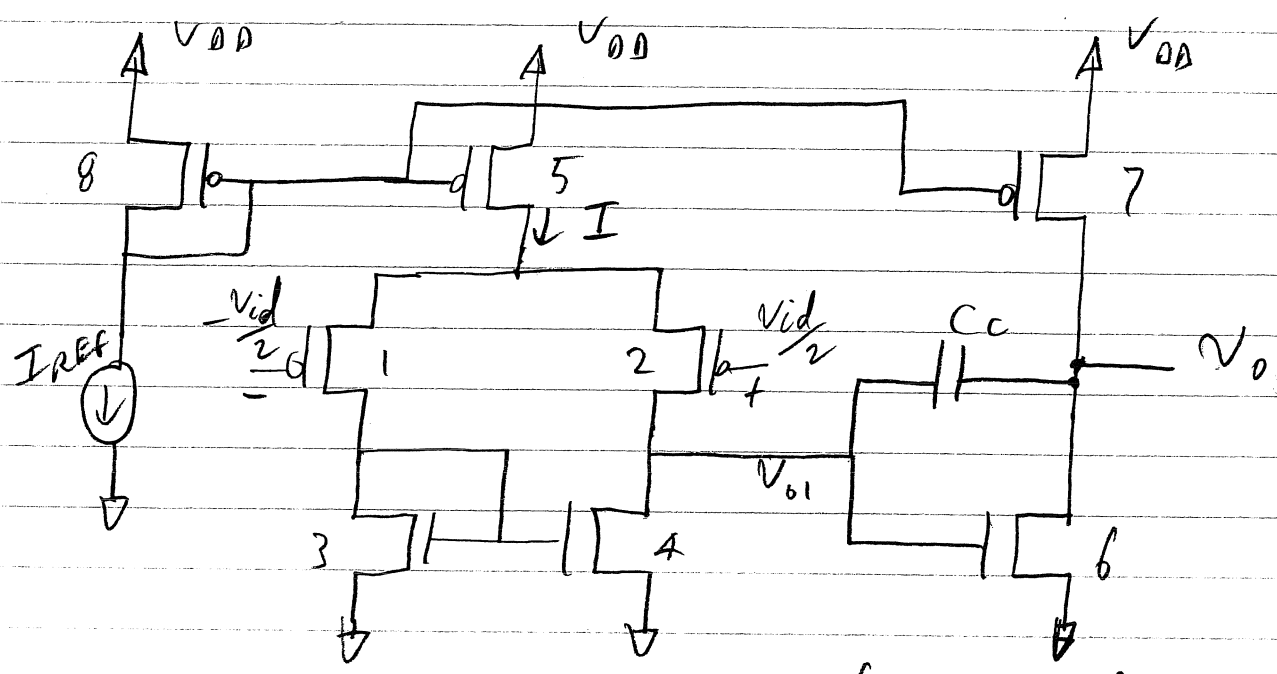
DIFFERENTIAL GAIN

$$A_d \equiv \frac{V_o}{V_{id}} = G_m R_o = g_m (\tau_{o2} \parallel \tau_{o4})$$

IF $\tau_o = \tau_{o2} = \tau_{o4}$

$$A_d = \frac{1}{2} g_m \tau_o$$

2 STAGE CMOS OPAMP



OVERALL GAIN $\frac{V_o}{V_{id}} = A_1 A_2$ (C_c IS A COMPENSATION CAP FOR STABILITY)

$$A_1 = \frac{V_{o1}}{V_{id}} = -g_{m1} (\tau_{o2} \parallel \tau_{o4})$$

$$A_2 = \frac{V_o}{V_{o1}} = -g_{m6} (\tau_{o6} \parallel \tau_{o7})$$

SIZING TRANSISTORS FOR ZERO SYSTEMATIC OFFSET

(RANDOM OFFSET WILL STILL OCCUR
↓ RESULT IN 1-20 mV INPUT
OFFSET VOLTAGE)

$$\text{LET } v_{id} = 0$$

SINCE M_3 & M_4 MATCHED

$$I_{D3} = I_{D4} = \frac{I}{2} \quad \downarrow \quad V_{DS3} = V_{DS4}$$

$$\text{SO } V_{GS6} = V_{DS4} = V_{DS3} = V_{GS3}$$

$$\Rightarrow I_{D6} = \frac{(W/L)_6}{(W/L)_3} \left(\frac{I}{2} \right)$$

FOR NO SYSTEMATIC OFFSET $I_{D7} = I_{D6}$

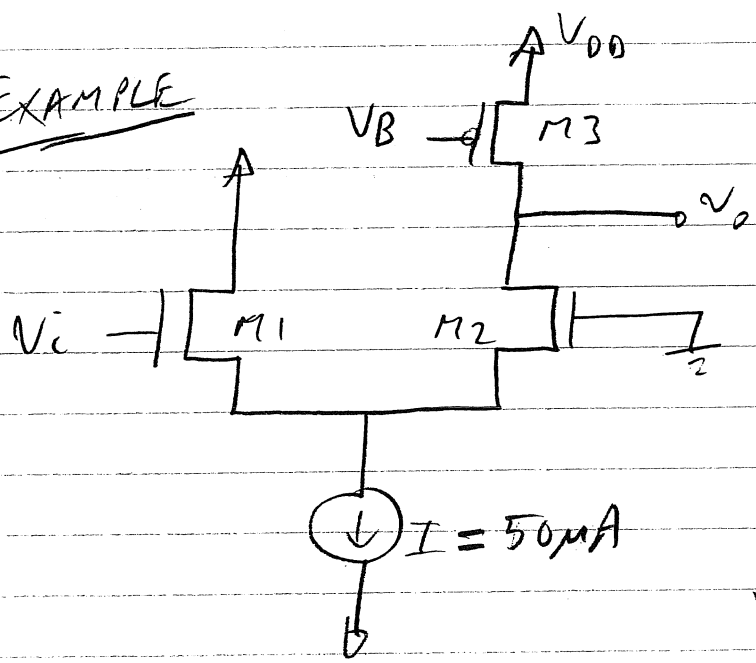
$$\downarrow \quad I_{D7} = \frac{(W/L)_7}{(W/L)_5} I$$

SO FOR $I_{D6} = I_{D7}$

$$\frac{(W/L)_6}{(W/L)_3} = 2 \frac{(W/L)_7}{(W/L)_5}$$

MD24

EXAMPLE



- $\mu_n \epsilon_{ox} = 290 \mu A/V^2$
- $\mu_p \epsilon_{ox} = 60 \mu A/V^2$
- $\lambda' = 0.1 \mu m/V$
- $V_{th} = 0.4 V$
- $W_1 = 2W_2 = 2 \mu m$
- $W_3 = 2 \mu m$
- ALL $L = 0.2 \mu m$

V_B CHOSEN SO $I_{D3} = I_{D2}$

FIND $\frac{V_o}{V_i}$

DC $I_{D1} = 2I_{D2} + I_{D1} + I_{D2} = I = 50 \mu A$

$I_{D2} = 16.7 \mu A$ $I_{D1} = 33.3 \mu A$

$g_{m1} = \sqrt{2 \mu_n \epsilon_{ox} \left(\frac{W_1}{L}\right) I_{D1}} = 400 \mu A/V$

$r_{s1} = 2.5 k \Omega$

$g_{m2} = 200 \mu A/V^2$ $r_{s2} = 5 k \Omega$

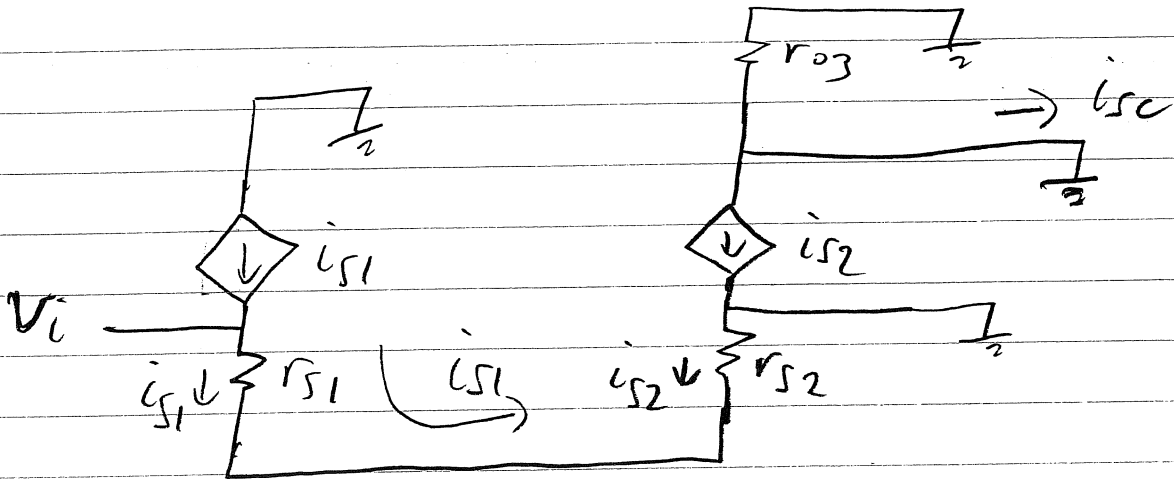
$r_{o1} = \frac{L}{\lambda' I_{D1}} = 60 k$ $r_{o2} = 120 k$

$V_{ov1} = V_{ov2} = 167 mV$

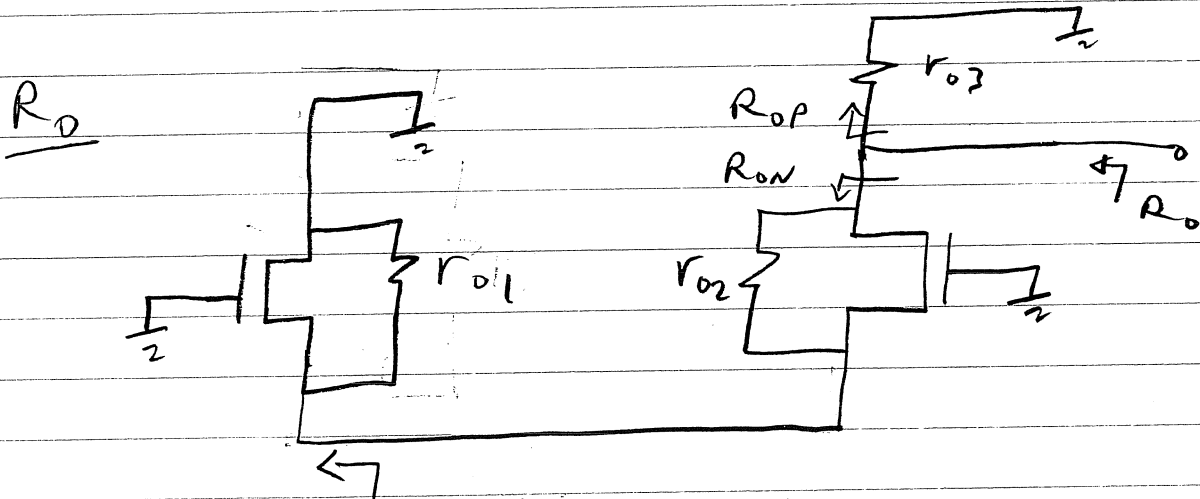
$r_{o3} = \frac{L}{\lambda' I_{D3}} = 120 k$

M025

Find i_{sc} (Ignore r_o)



$$i_{sc} = -i_{S2} = i_{S1} = \frac{V_i}{r_{S1} + r_{S2}} = \frac{V_i}{7.5k}$$



$$R_{i1} = r_{01} \parallel r_{S1} = 2.4k$$

$$R_{op} = r_{03} = 120k$$

$$R_{ow} = R_{i1} + r_{02} + \beta r_{02} R_{i1} = 180k$$

$$R_o = R_{op} \parallel R_{ow} = 72k$$

MD26

$$V_o = i_{sc} R_o = (72k) \left(\frac{V_i}{7.5k} \right)$$

$$\frac{V_o}{V_i} = 9.6 \text{ V/V}$$
