

Linearizability

- A Quick Overview

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These slides are modified versions of slides from Michael Freedman & Wyatt Lloyd's course on Distributed Systems

Data Consistency Models

- Contract (or a set of guarantees) that a system provides to applications about expected behavior when data is accessed (read, written, updated, etc.)

Linearizability

- Assumption: Each operation accesses one data item
- All operations are performed in some **total** order
- The total order preserves the **real-time ordering** between operations
 - If operation A **completes** before operation B **begins** in real-time, then A is ordered before B
 - If neither A nor B completes before the other begins, then there is no real-time order, but there must be some total order

Understanding Linearizability

- Writes are ordered
 - Writes appear to occur instantaneously
- Reads read latest data
 - After a write completes, a later read (in real-time order) returns the value of the write (or later write)
 - Once a read returns a value, all later reads return that value or the value of a later write

Real-Time Ordering Examples

$P_A \vdash w(x=1) \dashv$

$P_B \quad \vdash w(x=2) \dashv$

$P_C \quad \quad \vdash w(x=3) \dashv$

$P_D \quad \quad \vdash w(x=4) \dashv \quad \vdash w(x=5) \dashv$

$P_E \quad \quad \quad \vdash w(x=6) \dashv$

Linearizable?

$P_A \vdash w(x=1) \dashv$

$P_B \quad \vdash w(x=2) \dashv$

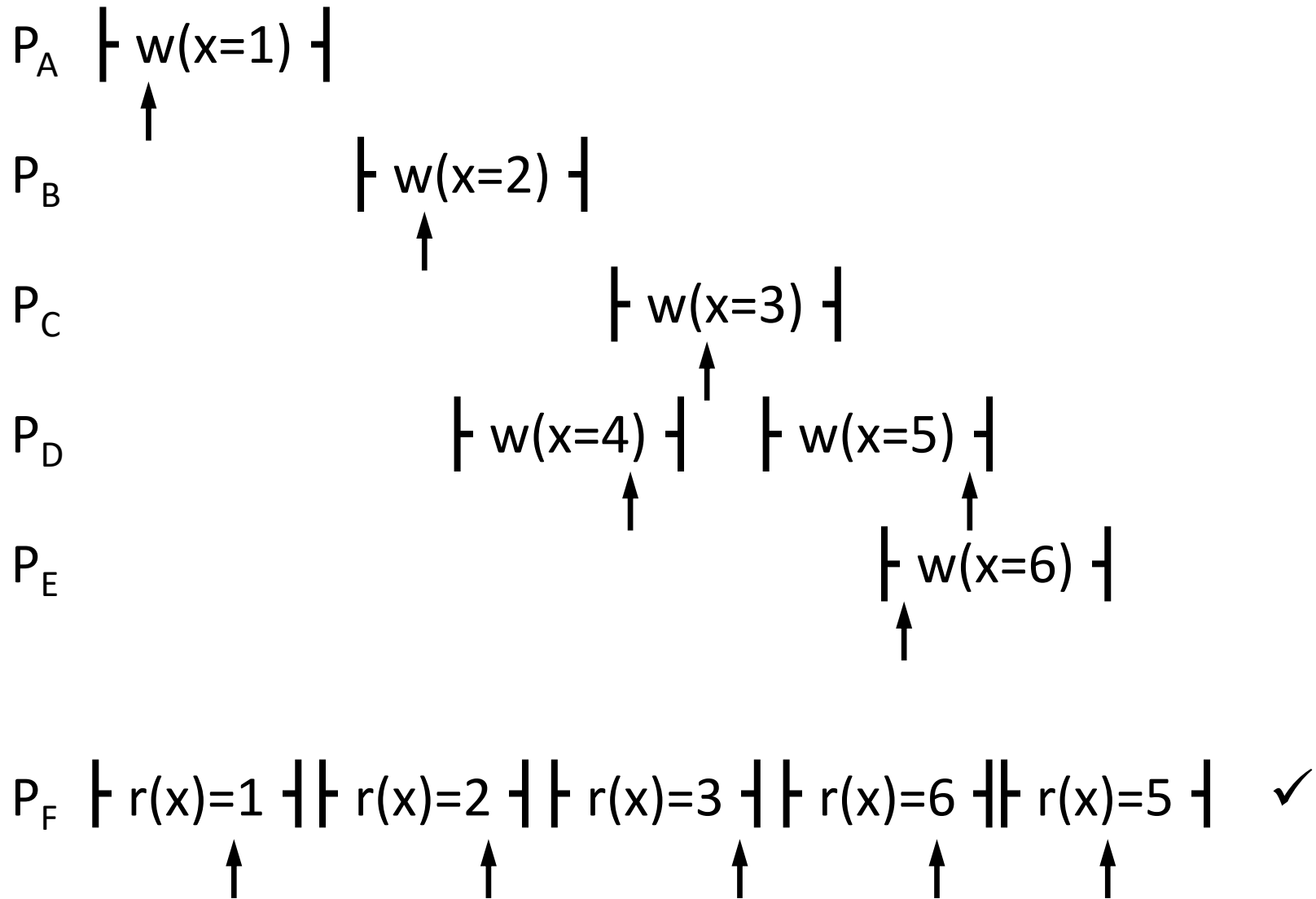
$P_C \quad \quad \vdash w(x=3) \dashv$

$P_D \quad \quad \vdash w(x=4) \dashv \quad \vdash w(x=5) \dashv$

$P_E \quad \quad \quad \vdash w(x=6) \dashv$

$P_F \vdash r(x)=1 \dashv \vdash r(x)=2 \dashv \vdash r(x)=3 \dashv \vdash r(x)=6 \dashv \vdash r(x)=5 \dashv$

Linearizable: Yes



Linearizable?

$P_A \vdash w(x=1) \dashv$

$P_B \quad \vdash w(x=2) \dashv$

$P_C \quad \quad \vdash w(x=3) \dashv$

$P_D \quad \quad \vdash w(x=4) \dashv \quad \vdash w(x=5) \dashv$

$P_E \quad \quad \quad \vdash w(x=6) \dashv$

$P_F \vdash r(x)=1 \dashv \vdash r(x)=2 \dashv \vdash r(x)=3 \dashv \vdash r(x)=6 \dashv \vdash r(x)=3 \dashv$

Linearizable: No

$P_A \vdash w(x=1) \dashv$

$P_B \vdash w(x=2) \dashv$

$P_C \vdash w(x=3) \dashv$

$P_D \vdash w(x=4) \dashv \vdash w(x=5) \dashv$

$P_E \vdash w(x=6) \dashv$
↑

$P_F \vdash r(x)=1 \dashv \vdash r(x)=2 \dashv \vdash r(x)=3 \dashv \vdash r(x)=6 \dashv \vdash r(x)=3 \dashv$
↑ ↑ stale read

Why Linearizability?

- Behavior is like single machine processing one request at a time
 - Hides the complexity of distributed and replicated systems from applications
 - Hides complexity associated with failures
 - Easier to write correct applications
- Atomic broadcast (Zab protocol used by ZooKeeper), RAFT, PAXOS, etc., provide linearizability for replicated data stores
- However, linearizability is a strong consistency guarantee that can limit performance
 - We will discuss this issue today